

MMN 31175

**NASA TECHNICAL  
MEMORANDUM**

**NASA TM-73,254**  
(Revised 8/30/78)

NASA TM-73,254

**A MATHEMATICAL FORCE AND MOMENT MODEL OF A UH-1H  
HELICOPTER FOR FLIGHT DYNAMICS SIMULATIONS**

**Peter D. Talbot and Lloyd D. Corliss**

**Ames Research Center, NASA**

**and**

**Ames Directorate, USAAMRDL, AVRADCOM  
Ames Research Center  
Moffett Field, Calif. 94035**

**June 1977**

## NOTATION

$a$	main rotor lift curve slope, per radian
$a_0$	main rotor coning, rad
$a_1, b_1$	first harmonic values of main rotor blade flapping with respect to control axis, rad
$a_{1s}, b_{1s}$	first harmonic values of main rotor blade flapping with respect to shaft axis, rad
$a_{1sw}$	longitudinal component of control axis position, rad
$A$	rotor disk area, $\pi R^2$ , ft <sup>2</sup> , m <sup>2</sup>
$A_{x,y,z}$	body axis accelerations, ft/sec <sup>2</sup> , m/sec <sup>2</sup>
$A_{1C}$	lateral swashplate control input, rad
$A_{1CB}$	lateral cyclic pitch contribution of stabilizer bar, rad
$A_{1CL}$	lateral swashplate control bias rigging term, rad
$A_{1CP}$	lateral pilot control input, rad
$A_{1s}$	lateral control axis command position with respect to shaft, rad
$b_{1sw}$	lateral component of control axis position, rad
$B_{1C}$	longitudinal swashplate control input, rad
$B_{1CB}$	longitudinal cyclic pitch contribution of stabilizer bar, rad
$B_{1CL}$	longitudinal swashplate control bias rigging term, rad
$B_{1CP}$	longitudinal pilot control input, rad
$B_{1s}$	longitudinal control axis command position with respect to shaft, rad
$C_1, C_4$	constants in linkage equations, cyclic stick to swashplate motion, rad/in., rad/cm
$C_5$	constant in linkage equation, collective pitch to collective stick motion, rad/in., rad/cm
$C_6, C_7$	constants in linkage equation, tail rotor collective pitch to pedal motion, rad/in., rad/cm

D	main rotor diameter, ft, m
$D_1, D_2, D_3$	constants in fuselage drag force equations, $\text{lb}/(\text{ft}/\text{sec})^2$ , $\text{N}/(\text{m}/\text{sec})^2$
$fe_1, fe_2, fe_3$	drag areas of fuselage, $\text{ft}^2$ , $\text{m}^2$
$F_1$	vertical fin drag constant, $\text{lb}/(\text{ft}/\text{sec})^2$ , $\text{N}/(\text{m}/\text{sec})^2$
$G_1$	constant used in ground effect computation
$\dot{h}$	helicopter rate of climb
$h_{\text{TR}}$	height of tail rotor above c.g., ft, m
H	rotor H-force in control axis - wind system, lb, N
$H_1, H_2, H_4$	constants in horizontal stabilizer aerodynamic forces, $\text{lb}/(\text{ft}/\text{sec})^2$ , $\text{N}/(\text{m}/\text{sec})^2$
$I_{xx}, I_{yy}, I_{zz}, I_{xz}$	inertias in body axis
$k_1, k_2$	constants in vertical fin aerodynamic forces, $\text{lb}/(\text{ft}/\text{sec})^2$ , $\text{N}/(\text{m}/\text{sec})^2$
$K_B$	numerator term, combining linkage and damping constants, of stabilizer bar input to cyclic pitch, sec
$K_G$	constant in $\lambda$ equation representing ground effect
$\ell_H$	waterline displacement of rotor hub from aircraft center of gravity, ft, m
$\ell_{\text{HS}}$	longitudinal displacement of horizontal stabilizer aerodynamic center from aircraft center of gravity, ft, m
$\ell_{\text{TR}}$	longitudinal displacement of tail rotor hub from aircraft center of gravity, ft, m
$\ell_{\text{VF}}$	waterline displacement of vertical fin aerodynamic center from aircraft center of gravity, ft, m
$L_1$	constant in fuselage aerodynamic force contribution, $\text{lb}/(\text{ft}/\text{sec})^2$ , $\text{N}/(\text{m}/\text{sec})^2$
$L_R$	body axis rolling moment, due to main rotor, ft-lb, J
$L_{\text{TR}}$	body axis rolling moment, due to tail rotor, ft-lb, J
$M_1$	constant in fuselage aerodynamic pitching moment, $\text{ft-lb}/(\text{ft}/\text{sec})^2$ , $\text{J}/(\text{ft}/\text{sec})^2$

$M_F$	body axis pitching moment, due to fuselage, ft-lb, J
$M_H$	body axis pitching moment, due to horizontal stabilizer, ft-lb, J
$M_R$	body axis pitching moment, due to main rotor, ft-lb, J
$N_1$	constant in fuselage aerodynamic yawing moment, ft-lb/(ft/sec) <sup>2</sup> , J/(m/sec) <sup>2</sup>
$N_F$	body axis yawing moment, due to fuselage, ft-lb, J
$N_R$	body axis yawing moment, due to main rotor, ft-lb, J
$N_{TR}$	body axis yawing moment, due to tail rotor, ft-lb, J
$N_{VF}$	body axis yawing moment, due to vertical fin, ft-lb, J
$P_B$	body axis roll rate, rad/sec
$P_C$	main rotor shaft roll rate, wind-control axis system, rad/sec
$Q$	main rotor torque, ft-lb, J
$q_B$	body axis pitch rate, rad/sec
$q_C$	main rotor shaft pitch rate, wind-control axis system, rad/sec
$r_B$	body axis yaw rate, rad/sec
$R$	rotor radius, ft, m
$R_1, R_2, \dots, R_9$	constants in main rotor force equations, table 3
(s)	Laplace operator
$S$	area of aerodynamic surface, ft <sup>2</sup> , m <sup>2</sup>
$T$	main rotor thrust, lb, N
$T_1, T_2, \dots, T_5$	constants in tail rotor force equations, table 3
$T_{TR}$	tail rotor thrust, lb, N
$u_B$	x-body axis relative velocity, ft/sec, m/sec
$u_C$	longitudinal component of relative wind in wind control axis system, ft/sec, m/sec
$u_F$	component of relative wind in equations for vertical fin aerodynamic force, ft/sec, m/sec

$u_H$	component of relative wind in equations for horizontal stabilizer aerodynamic force, ft/sec, m/sec
$v_B$	y-body axis relative velocity, ft/sec, m/sec
$v_C$	lateral component of relative wind in wind-control axis system, ft/sec, m/sec
$v_F$	component of relative wind in equations for vertical fin aerodynamic force, ft/sec, m/sec
$v_T$	relative wind normal to plane of tail rotor, ft/sec, m/sec
$w_B$	z-body axis relative velocity, ft/sec, m/sec
$w_C$	vertical component of relative wind in wind-control axis system, ft/sec, m/sec
$w_H$	component of relative wind in equations for horizontal stabilizer aerodynamic force, ft/sec, m/sec
$X_C$	main rotor force in control axis system, lb, N
$X_F$	longitudinal x-body force, due to fuselage, lb, N
$X_R$	longitudinal x-body force, due to main rotor, lb, N
$X_{c.g.}$	longitudinal distance of aircraft center of gravity forward of main rotor shaft hub, ft, m
$Y$	rotor Y-force in wind control axis system, lb, N
$Y_1$	constant in fuselage aerodynamic force contribution, lb, N
$Y_C$	main rotor force in control axis system, lb, N
$Y_F$	lateral y-body force, due to fuselage, lb, N
$Y_R$	lateral y-body force, due to main rotor, lb, N
$Y_{TR}$	lateral y-body force due to tail rotor, lb, N
$Y_{VF}$	lateral y-body force, due to vertical fin, lb, N
$Z$	rotor height above ground plane, ft, m
$Z_C$	main rotor force in control axis system, lb, N
$Z_F$	vertical z-body force, due to fuselage, lb, N

$Z_H$	vertical z-body force, due to horizontal stabilizer, lb, N
$Z_R$	vertical z-body force, due to main rotor, lb, N
$\alpha_F$	vertical fin angle of attack, rad
$\alpha_{HS}$	horizontal stabilizer angle of attack, rad
$\beta_m$	maximum flapping amplitude of main rotor with respect to shaft, rad
$\gamma$	rotor Lock number for one blade, $\rho \frac{aCR^4}{I_\beta}$
$\delta$	rotor mean blade drag coefficient
$\delta_0, \delta_2$	constants in rotor drag equation
$\delta_{1B}, \delta_{2B}$	stabilizer bar flapping constants, rad
$\delta_a$	pilot's lateral stick displacement, in., cm
$\delta_c$	pilot's collective stick displacement, in., cm
$\delta_e$	pilot's longitudinal stick displacement, in., cm
$\delta_p$	pilot's pedal displacement, in., cm
$\delta_s$	horizontal stabilizer incidence angle, rad
$\theta$	aircraft pitch attitude Euler angle, deg, rad
$\theta_0$	main rotor collective pitch
$\theta_{TR}$	tail rotor collective pitch, rad
$\lambda$	main rotor inflow ratio
$\mu$	main rotor advance ratio
$\rho_0$	sea level air density, slugs/ft <sup>3</sup> , kg/m <sup>3</sup>
$\sigma$	rotor solidity
$\tau_B$	stabilizer bar time constant, sec
$\tau_R$	control axis response time constant, sec
$\phi$	aircraft roll attitude, rad
$\phi_c$	amplitude of total cyclic pitch control input, rad
$\phi_p$	phase angle of cyclic rigging, deg

$\phi_t$  phase (with respect to body axis) of total cyclic pitch control input, rad

$\psi$  aircraft heading, rad

$\Omega$  rotor rotational speed, rad/sec

#### Subscripts

TR tail rotor

VF vertical fin

HS horizontal stabilizer

IC initial conditions - trimmed conditions for the helicopter

m model

A MATHEMATICAL FORCE AND MOMENT MODEL OF A UH-1H  
HELICOPTER FOR FLIGHT DYNAMICS SIMULATIONS

Peter D. Talbot and Lloyd D. Corliss

Ames Research Center, NASA  
and  
Ames Directorate, USAAMRDL, AVRADCOM

SUMMARY

A model of a Bell UH-1H helicopter was developed to support several simulations at Ames Research Center and was used also for development work on an avionics system known as the V/STOLAND system at Sperry Flight Systems. This report presents the complete equations and numerical values of constants used to represent the helicopter.

Responses to step inputs of the cyclic and collective controls are shown and compared with flight test data for a UH-1H. The model coefficients were adjusted in an attempt to get a consistent match with the flight time histories at hover and 60 knots. Fairly good response matching was obtained at 60 knots, but the matching at hover was not as successful. Pilot evaluations of the model, both fixed and moving base, were made.

INTRODUCTION

The mathematical force and moment model described was developed to satisfy the need for representing the dynamics of a UH-1H helicopter for piloted simulation. The model was developed specifically for use in flight dynamics investigations and for simulation of terminal-area guidance and navigation tasks. It has been used in simulations for the development of software for the navigation and guidance programs of an avionics system known as V/STOLAND and for the investigation of the effects of failures of stability augmentation elements of the control system (see ref. 1).

The equations, representing the nonlinear contributions of the components of the helicopter to the force and moments were assembled from many sources. The equations are in general form so that changes can be made to represent helicopters other than the UH-1H. The model employs a quasi-static main rotor representation, uniform inflow over the rotor disc, and simple expressions for the contributions of the tail rotor, fuselage, and empennage. No interference effects between components were modelled. In the simulation, the equations were used in a standard digital program, partially described in reference 2 which incorporates the equations of motion, variations in the atmosphere, and routines for interfacing with analog equipment for

driving instruments, providing control forces, etc. Simulations have been conducted with an EAI 8400 computer.

The model was evaluated by comparing its response to step inputs with those obtained in flight on a UH-1H helicopter, and subjective pilot assessments. The pilot evaluations were obtained during both fixed and moving-base simulations.

## HELICOPTER FORCE AND MOMENT EQUATIONS

The quasi-static main rotor equations were adapted from reference 3. The equations for the aerodynamic forces of the fuselage and empennage were separately derived, based either on available wind tunnel data of reference 4 or standard textbook wing theory, modified to approximate stalled conditions. An approximate representation for the tail rotor was derived; however, in its original form it did not correctly predict tail rotor damping. The form of the equations was retained with adjusted constant values used to match the apparent tail rotor damping seen in the flight test data yaw responses.

The equations represent aerodynamic forces and moments contributed by each component of the helicopter. The net results are three aerodynamic forces and three aerodynamic moments applied in a body-axis system. The origin of the body system is the helicopter c.g. The z axis of the reference frame was taken to be parallel to the main rotor shaft, positive direction down, as in figure 1.

The constant values used for the coefficients in the equations are presented in tables 1 and 2. It may be noted that the characteristic lengths used to compute moments are based on data referenced to the waterline-buttlene-station system of the helicopter, rather than the axis system defined above. Since the UH-1H has a 5° forward mast tilt, slight discrepancies are introduced by using raw station and waterline values to locate components of the model. These are thought to be insignificant.

### Main Rotor Forces at the Rotor Hub

$$T = R_1 \left[ \theta_o \left( \frac{1}{3} + \frac{\mu^2}{2} \right) + \frac{\lambda}{2} + R_2 \mu p_C \right] \quad (1)$$

$$H = R_1 \left\{ R_3 \delta \mu + a_1 \left[ \frac{\theta_o}{3} + \frac{3}{4} \lambda \left( 1 - \frac{3}{8} \mu^2 \right) + \frac{\mu a_1}{4} \right] - \frac{\mu \lambda \theta_o}{2} \left( \frac{1 - 2\mu}{3\pi} \right) - \frac{\lambda^2 \mu}{4} \right. \\ \left. - \frac{3}{8} \lambda \mu^2 (1 + 3.33\mu) - a_o \left( \frac{b_1}{6} - \frac{a_o \mu}{4} \right) - R_4 q_C \left( \frac{a_o}{6} + \frac{\mu b_1}{16} \right) \right. \\ \left. - R_4 p_C \left( \frac{\theta_o}{6} + \frac{\lambda}{2} \right) + \frac{\mu a_1}{16} \right\} \quad (2)$$

$$Y = R_1 \left\{ a_o \left[ a_1 \left( \frac{1}{6} - \mu^2 \right) - \frac{3}{2} \mu \left( \lambda + \frac{\theta_o}{2} \right) \right] + b_1 \left[ \frac{\theta_o}{3} \left( 1 + \frac{3}{2} \mu^2 \right) + \frac{3}{4} \lambda + \frac{\mu a_1}{4} \right] + R_4 q_C \left( \frac{\theta_o}{6} + \frac{\lambda}{2} + \frac{7}{16} \mu a_1 \right) - R_4 p_C \left( \frac{a_o}{6} - \frac{5}{16} \mu b_1 \right) \right\} \quad (3)$$

#### Main Rotor Torque

$$Q = R_9 \left[ R_5 \delta (1 + \mu^2) - \frac{\lambda \theta_o}{3} - \frac{\lambda^2}{2} - \frac{1}{8} (a_1^2 + b_1^2) - \frac{\mu^2}{2} \left( \frac{a_o^2}{2} + \frac{3}{8} a_1^2 + \frac{b_1^2}{8} \right) - \frac{\mu \lambda a_1}{2} + \frac{\mu a_o b_1}{3} \right] \quad (4)$$

This expression was obtained from reference 5, equation (44), p. 195.

#### Flapping Coefficients

$$a_o = 0.048 \quad (5)$$

$$a_1 = \frac{1}{1 - \mu^2/2} \left[ \mu \left( \frac{8}{3} \theta_o + 2\lambda \right) + R_4 p_C - R_6 q_C \right] \quad (6)$$

$$b_1 = \frac{1}{1 + \mu^2/2} \left( \frac{4}{3} \mu a_o - R_4 q_C - R_6 p_C \right) \quad (7)$$

#### Advance Ratio

$$\mu = \left( u_C^2 + v_C^2 \right)^{1/2} R_7 \quad (8)$$

#### Mean Blade Drag Coefficient

$$\delta = \delta_o + \delta_2 T^2 \quad (9)$$

#### Inflow Ratio

This expression is an implicit function and required an iterative solution in the computer program.

$$\lambda = -R_7 w_C - \frac{R_8 T}{(\mu^2 + \lambda^2)^{1/2}} K_G \quad (10)$$

The  $K_G$  factor is a ground effect term and represents a reduction in inflow velocity in ground effect. The value  $G_1$  (below) was adjusted to match performance data presented in reference 6.

$$K_G = 1 - e^{(-Z/D)/G_1} \quad (10a)$$

Wind Components at the Rotor Hub

$$u_C = -u_B - w_B B_{1S} + q_B l_H \quad (11)$$

$$v_C = -v_B - w_B A_{1S} - p_B l_H \quad (12)$$

$$w_C = -w_B + B_{1S}(u_B - q_B l_H) + A_{1S}(v_B + p_B l_H) \quad (13)$$

Rotor Forces and Moments Resolved Into Body Axes

(a) Forces in control axis system

$$X_C = \frac{Hu_C}{(u_C^2 + v_C^2)^{1/2}} + \frac{Yv_C}{(u_C^2 + v_C^2)^{1/2}} \quad (14)$$

$$Y_C = \frac{Hv_C}{(u_C^2 + v_C^2)^{1/2}} - \frac{Yu_C}{(u_C^2 + v_C^2)^{1/2}} \quad (15)$$

$$Z_C = -T \quad (16)$$

(b) Main rotor forces in body axes

$$X_R = X_C - Z_C B_{1S} \quad (17)$$

$$Y_R = Y_C - Z_C A_{1S} \quad (18)$$

$$Z_R = Z_C + X_C B_{1S} + Y_C A_{1S} \quad (19)$$

(c) Main rotor moments in body axes

$$L_R = Y_R \ell_H \quad (20)$$

$$M_R = -X_R \ell_H + Z_R X_{c.g.} \quad (21)$$

$$N_R = Q - Y_R X_{c.g.} \quad (22)$$

Pilot to Swashplate Control Equations

$$A_{1CP} = C_4 \delta_a \quad (23)$$

$$B_{1CP} = C_1 \delta_e \quad (24)$$

In this form, no cross-coupling is shown corresponding to control rigging. In the most general form,

$$A_{1CP} = C_4 \delta_a \cos \phi_p - C_1 \delta_e \sin \phi_p \quad (25)$$

$$B_{1CP} = C_4 \delta_a \sin \phi_p + C_1 \delta_e \cos \phi_p \quad (26)$$

For the UH-1H  $\phi_p$  is actually  $5^\circ$ . For the simulation  $\phi_p = 0^\circ$  was used.

Main and Tail Rotor Collective Pitch

$$\theta_o(s) = \frac{C_5 \delta_c}{\tau_c s + 1} \quad (27)$$

The first order lag representation was used to match more closely the  $a_z$  acceleration data obtained from the flight test results.

$$\theta_{TR} = C_6 \delta_p + C_7 \quad (28)$$

Stabilizer Bar Transfer Functions

The Bell stabilizer bar can be represented by a simple transfer function which describes its parallel input to the cyclic pitch of the main rotor. It is characterized by a gain  $K_B$  and a time constant,  $\tau_B$ , which reflect

respectively the mechanical mixing ratio and the mechanical damper characteristic of the shaft-mounted bar.

$$B_{1CB}(s) = \frac{K_B}{\tau_B s + 1} q_B(s) \quad (29)$$

$$A_{1CB}(s) = \frac{-K_B}{\tau_B s + 1} p_B(s) \quad (30)$$

The bar has a pronounced effect on the stability and control characteristics of the helicopter. Values of the bar constants were obtained by consultation with Bell Helicopter Company.

#### Control Inputs to Cyclic Pitch

The control inputs to the rotor cyclic pitch are represented as the sum of those due to the pilot, stabilizer bar and rigging of the control system.

$$B_{1C} = B_{1CP} + B_{1CB} + B_{1CL} \quad (31)$$

$$A_{1C} = A_{1CP} + A_{1CB} + A_{1CL} \quad (32)$$

#### Rotor Control Axis Response to Cyclic Pitch

In this representation,  $A_{1C}$  and  $B_{1C}$  are regarded as inputs to the rotor cyclic pitch. The control axis of the helicopter is then allowed to follow with a lag related to the rotor Lock number. The terms  $A_{1S}$  and  $B_{1S}$  represent the instantaneous orientation of the control axis with respect to the fuselage body axis system (in this case, the main rotor shaft axis).

$$B_{1S}(s) = \frac{B_{1C}(s)}{\tau_R s + 1} \quad (33)$$

$$A_{1S}(s) = \frac{A_{1C}(s)}{\tau_R s + 1} \quad (34)$$

In steady state,  $B_{1S} = B_{1C}$  and  $A_{1S} = A_{1C}$ .

Thrust  $T$  is oriented along the control axis and the  $H$  and  $Y$  forces are orthogonal to  $T$  and each other. Forces  $H$  and  $Y$  may be viewed approximately as components of the rotor force normal to the tip path plane arising from rotor tip path plane excursions from the commanded control axis

position (as in ref. 7) or as unique forces derived in a consistent wind-control axis system as in reference 3. In this representation, reference 3 was followed. Equations 14 through 19 resolve the T, H and Y forces into body axes.

#### Control Axis Pitch and Roll Rates

In equations (1) through (7) the terms  $q_C$  and  $p_C$  are used to denote pitch and roll rates of the control axis in the control axis-wind system. They are related to the body pitch and roll rates by the following two equations:

$$p_C = -p_B \frac{u_C}{(u_C^2 + v_C^2)^{1/2}} - q_B \frac{v_C}{(u_C^2 + v_C^2)^{1/2}} \quad (35)$$

$$q_C = -q_B \frac{u_C}{(u_C^2 + v_C^2)^{1/2}} + p_B \frac{v_C}{(u_C^2 + v_C^2)^{1/2}} \quad (36)$$

#### Tail Rotor Thrust

$$T_{TR} = \left[ -T_2 + (T_2^2 + T_3 |\theta_{TR}|)^{1/2} \right]^2 \frac{\theta_{TR}}{|\theta_{TR}|} \left( 1 + T_1 \frac{|u_B|}{\theta_2} \right) - (T_4 + T_5 |u_B|) v_T \quad (37)$$

where

$$\theta_2 = |\theta_{TR}| \quad , \quad \theta_{TR} > 0.0873$$

$$\theta_2 = 0.0873 \quad , \quad \theta_{TR} \leq 0.0873$$

$$v_T = v_B - r_B \ell_{TR} + p_B h_{TR} \quad (38)$$

Due to memory limitations in the computer, these equations were originally derived as an economical approximation to the tail rotor thrust of an isolated tail rotor. (The equations do not incorporate the vortex ring operating state of the tail rotor or fin interference effects.) They reflect the main influences of inflow and collective pitch on tail rotor thrust. It was found that the derivation on which  $T_4$  was based, grossly underpredicted the tail rotor damping contribution to  $N_r$ . It was necessary, therefore, to adjust the constant empirically to match the flight test results.

Tail Rotor Contribution to Body Forces and Moments

$$Y_{TR} = T_{TR} \quad (39)$$

$$L_{TR} = Y_{TR} h_{TR} \quad (40)$$

$$N_{TR} = -Y_{TR} \ell_{TR} \quad (41)$$

Fuselage Aerodynamics

$$X_F = u_B \left( -D_1 |u_B| + L_1 \frac{w_B^2}{|u_B|} \right) \quad (42)$$

$$Y_F = v_B \left( -D_2 |v_B| - Y_1 |u_B| \right) \quad (43)$$

$$Z_F = w_B \left( -D_3 |w_B| - L_1 |u_B| \right) \quad (44)$$

$$M_F = M_1 w_B |u_B| \quad (45)$$

$$N_F = -N_1 v_B u_B \quad (46)$$

Vertical Fin Aerodynamics

$$u_F = u_B \quad (47)$$

$$v_F = -v_B + \ell_{VF} r_B \quad (48)$$

$$\sin \alpha_F = v_F / (u_F^2 + v_F^2)^{1/2} \quad (49)$$

$$Y_{VF} = K_1 v_F u_F + F_1 v_F |v_F| \quad \begin{array}{l} -20^\circ \leq \alpha_F \leq 20^\circ \\ 160^\circ \leq \alpha_F \leq 200^\circ \end{array} \quad (50)$$

$$Y_{VF} = k_2 u_F^2 + F_1 v_F |v_F| \quad 20^\circ < \alpha_F < 160^\circ \quad (51)$$

$$Y_{VF} = -k_2 u_F^2 + F_1 v_F |v_F| \quad 200^\circ < \alpha_F < 340^\circ \quad (52)$$

$$N_{VF} = -Y_{VF} \ell_{VF} \quad (53)$$

### Horizontal Stabilizer Aerodynamics

$$w_H = w_B + \frac{\lambda}{R_7} + u_B \delta_s + \ell_{HS} q_B + w_C \quad (54)$$

$$u_H = u_B \quad (55)$$

The horizontal stabilizer of the helicopter is connected to the longitudinal cyclic control and varies in a nonlinear manner with longitudinal cyclic stick position (table 1).

At the time these equations were developed, data for the UH-1H stabilizer incidence schedule were not available. Since the UH-1B stabilizer is linked in a similar manner to the cyclic controls, and table 1 values were available, they were used in lieu of UH-1H values.

$$\sin \alpha_{HS} = \frac{w_H}{(u_H^2 + w_H^2)^{1/2}} \quad (56)$$

$$Z_H = -H_1 w_H u_H - H_4 w_H |w_H| \quad \begin{array}{l} -20^\circ \leq \alpha_{HS} \leq 20^\circ \\ 160^\circ \leq \alpha_{HS} \leq 200^\circ \end{array} \quad (57)$$

$$Z_H = -H_2 u_H^2 - H_4 w_H |w_H| \quad 20^\circ < \alpha_{HS} < 160^\circ \quad (58)$$

$$Z_H = H_2 u_H^2 - H_4 w_H |w_H| \quad 200^\circ < \alpha_{HS} < 340^\circ \quad (59)$$

$$M_H = Z_H \ell_{HS} \quad (60)$$

### Total Body Forces and Moments

$$x_B = X_R + X_F \quad (61) \quad L_B = L_R + L_{TR} \quad (64)$$

$$Y_B = Y_R + Y_{TR} + Y_F + Y_{VF} \quad (62) \quad M_B = M_R + M_F + M_H \quad (65)$$

$$Z_B = Z_R + Z_F + Z_H \quad (63) \quad N_B = N_R + N_{TR} + N_F + N_{VF} \quad (66)$$

The form of the equations for the fuselage, horizontal stabilizer and vertical fin aerodynamics results from using trigonometric functions to approximate the lift and drag curves in wind axes, and then resolving these forces and relative wind into body axes.

## Estimation of Rotor Flapping with Respect to the Shaft

The tip path plane orientation with respect to the control axis is represented by the values of the flapping coefficients  $a_1$  and  $b_1$ . As an approximation to the actual rotor flapping angle with respect to the shaft  $a_{1s}$  and  $b_{1s}$ , the following equations were used. They reflect the influences of the cyclic control inputs  $A_{1C}$  and  $B_{1C}$  and the computed flapping amplitudes  $a_1$  and  $b_1$ . The sign convention of reference 5 is followed.

$$a_{1s} = a_1 - b_{1sw} \quad (67)$$

$$b_{1s} = b_1 + a_{1sw} \quad (68)$$

$$a_{1sw} = \phi_c \cos \phi_t \frac{v_C}{(u_C^2 + v_C^2)^{1/2}} - \phi_c \sin \phi_t \frac{u_C}{(u_C^2 + v_C^2)^{1/2}} \quad (69)$$

$$b_{1sw} = -\phi_c \sin \phi_t \frac{v_C}{(u_C^2 + v_C^2)^{1/2}} - \phi_c \cos \phi_t \frac{u_C}{(u_C^2 + v_C^2)^{1/2}} \quad (70)$$

$$\phi_c = \cos^{-1}(\cos A_{1C} \cos B_{1C}) \quad (71)$$

$$\phi_t = \tan^{-1} \left( \frac{\tan A_{1C}}{\sin B_{1C}} \right) \quad (72)$$

The maximum flapping amplitude is given by

$$\beta_m = (a_{1s}^2 + b_{1s}^2)^{1/2} \quad (73)$$

where  $\beta_m$  is the maximum teetering angle with respect to the rotor mast. The orthogonal components of flapping in the wind-shaft axis system are  $a_{1s}$  and  $b_{1s}$ , and  $\phi_c$  and  $\phi_t$  are the amplitude of the cyclic input and the phase of the cyclic input, respectively.

### COMPARISON OF HELICOPTER FLIGHT DYNAMICS WITH MATH MODEL DYNAMICS

A Bell UH-1H helicopter was instrumented and flown at Crows Landing NAS November 12, 1974 for the purpose of obtaining flight records against which the simulator model could be compared.

In this section, the helicopter responses to step control inputs are compared directly with the math model responses to the same inputs.

### Flight Conditions

Two flight conditions are shown: hover out of ground effect and 60 knots level flight. The flight tests were made at nominally sea level no-wind conditions. The simulator model is shown at standard day, sea level conditions.

### Control Inputs

Step control inputs of from  $\pm 1.25$  cm to  $\pm 2.5$  cm ( $\pm 1/2$  in. to  $\pm 1$  in.) were made in collective, pitch, roll, and yaw controls. The pilot was instructed to establish a steady flight condition (zero rate of climb, pitch, roll, and yaw) and then to input and hold the appropriate control for as long a period as possible before initiating a recovery. These inputs are simulated as true steps in the simulator time history comparisons. Amplitudes for the simulator inputs are adjusted to conform as closely as possible to the flight values for linear displacements at the pilot's hand or foot.

### Aircraft Configuration

The aircraft flown, and the simulator model, represents a standard UH-1H (with stabilizer bar) weighing 2800 kg (6158 lb). This weight is the estimated initial gross weight of the helicopter at the commencement of the tests. Both the weight and longitudinal center of gravity were derived from a pre-flight weight and balance of the helicopter, followed by adjustments for fuel burnoff and personnel transfers prior to the test runs.

The inertia values used for the simulator model are representative values obtained from unpublished Bell Helicopter Company data.

The vertical center of gravity of the helicopter was not known. The characteristic lengths used in the model reflect only a reasonable estimate of its value.

### Aircraft On-Board Sensors

The sensors on the aircraft were:

1. Body angular rate gyros sensing roll rate, pitch rate and yaw rate,
2. Vertical gyro sensing Euler attitudes of the aircraft in roll, pitch, and heading,
3. Body accelerometers measuring body axis accelerations,

4. Airspeed indicator,
5. Instantaneous vertical speed indicator (IVSI), i.e., rate-of-climb pressure instrument,
6. Sensors for measuring control displacements at the pilot's hand or foot:  $\delta_c$  (collective pitch stick),  $\delta_e$  (longitudinal cyclic stick),  $\delta_a$  (lateral cyclic stick), and  $\delta_p$  (pedal, or  $\theta_{TR}$  pitch input).

#### Time History Comparisons

The aircraft and model angular rate and attitude responses to the step control inputs are shown opposite each other in figures 2 through 9. Figures 2 through 5 are responses to inputs initiated from a steady 60 knot trimmed forward flight condition. Figures 6 through 9 are responses to inputs starting from an initial trimmed hover condition.

The format for each figure is the same. The first page consists of  $p_B$ ,  $q_B$  and  $r_B$  versus time for the control input shown at the bottom of the page. The second page shows the displacement angles  $\phi$ ,  $\theta$  and  $\psi$  and the vertical acceleration  $A_z$  for the same control input. Vertical lines on the flight data denote the beginning and end of the control input. Tick marks on the model data indicate control input. All pens are zeroed at the end of the control step on the model data.

The aircraft  $A_z$  is included only for a general trend comparison since the filtering of this signal was subsequently found to be questionable. The aircraft IVSI was suspected of having a large lag since radar height position data did not compare well with integrated instantaneous vertical speed indicator (IVSI) readings. Consequently, a comparison of rate-of-climb response to collective pitch is not shown. Comparison with radar height data in hover did show that the rate-of-climb response is a first order type of heave response ( $h = K_h \delta_c (1 - e^{-t/\tau_h})$ ) and that both the time constant and steady state values were well modeled by the equations.

A direct comparison of the records at 60 knots shows that the primary responses to the control inputs are reasonably well modeled: pitch rate to longitudinal cyclic, roll rate to lateral cyclic and yaw rate to a pedal step. The coupled responses to these same steps show sign differences in some cases, but the absolute magnitudes of the responses are small. For the pedal step and the collective step, where the coupled responses are larger, the magnitudes and signs of the coupled responses appear to be properly represented.

Attempts to duplicate flight responses in hover were not as successful. The primary responses are sufficiently well modeled so that the pilot was given proper cues in the first one to two seconds following a servo failure. The long term response in pitch rate is exaggerated and the long term response in roll rate is underpredicted by the model. In addition, strong pitch coupling is evident in the flight records for both the lateral step

input and the pedal step input, a phenomenon not present in the model. The physical reason for these coupled responses was not understood.

The primary yaw rate response in hover is good. The coupled yaw responses to lateral cyclic pitch and to collective pitch are satisfactory.

The validation effort was stopped at this point because further attempts to improve the hover responses were not successful, or it changed the model adversely at 60 knots. Without more insight into the basic aerodynamics of the aircraft in hover, it was also difficult to understand how to alter the equations to obtain the desired results.

The initial responses to servo hardovers were believed realistic enough to provide the pilot with the appropriate cues to initiate recovery. The overall dynamics appeared to be adequate to give a reasonable estimate of aircraft excursions during the recovery from a failure.

### Pilot Evaluations

In addition to comparing the model with flight time histories, the model was operated both in a fixed-base simulator and in a six-degree-of-freedom moving-base simulator (6 DOF). The model was flown with and without motion washout in hover, and with motion washout at 60 knots. The flights without washout were made with open cab and with real outside-world references. The flights with washout, and fixed base, were made with visual reference provided by a terrain model.

The model was judged to be realistic at 60 knots by the research pilots who flew the simulation. However, the model was judged to be difficult to fly normally in hover by every pilot who flew it. Precise hover and precise maneuvers around hover at low speeds, including quick stops and lateral translations, were more difficult with the simulated model than with the actual helicopter. Motion cues provided by the 6 DOF simulator did not change the pilot's evaluations.

In spite of this, all pilots were able to adapt themselves to the simulator and fly quite precisely after a learning period. Precision hover in the 6 DOF simulator with open cab and no motion washout was possible. In addition to this, recoveries from roll and pitch servo hardovers were accomplished, and a precision hover reestablished within the 5.5 m<sup>2</sup> of possible simulator travel.

This model was used in a flight control simulation described in reference 1.

## CONCLUDING REMARKS

The mathematical model of a UH-1H helicopter described in this report was developed for real time piloted simulation. The model was evaluated by comparing its dynamics objectively with flight test results and subjectively with pilot evaluations. The model appears to be satisfactory for flying qualities investigations at forward speeds and usable, but less realistic, for hover. The reasons for the discrepancies between flight and simulation have not yet been determined.

It is believed that enough information has been provided here to enable a potential user to decide whether the model is suitable for his application.

## REFERENCES

1. Corliss, Lloyd C.; and Talbot, P. D.: A Failure Effects Simulation of a Low Authority Flight Control Augmentation System on a UH-1H Helicopter. NASA TM-73,258, 1977.
2. McFarland, R. F.: A Standard Kinematic Model for Flight Simulation at NASA-Ames. NASA CR-2497, 1975.
3. Seckel, Edward; and Curtiss, H. C., Jr.: Aerodynamic Characteristics of Helicopter Rotors. Rotor Contributions to Helicopter Stability Parameters. Princeton University Report, 1963.
4. Biggers, J. C.; McCloud, J. L., III; and Patterakis, Peter: Wind Tunnel Tests of Two Full Scale Helicopter Fuselages. NASA TN D-1548, 1962.
5. Gessow, A.; and Myers, G. C., Jr.: Aerodynamics of the Helicopter. Macmillan, 1952.
6. Flanigen and Porter: Category II Performance Tests of the YUH-1D with a 48-foot Rotor. AFFTC TDR 64-27, Nov. 1964.
7. Wilcock, T.; and Thorpe, A. C.: Flight Simulation of a Wessex Helicopter: A Validation Exercise. RAE TR 73096, Sept. 1973.
8. McCloud, J. L., III; Biggers, J. C.; and Stroub, R. H.: An Investigation of Full Scale Helicopter Rotors at High Advance Ratios and Advancing Tip Mach Numbers. NASA TN D-4632, 1968.
9. Finnestead, R. L.; and Graham, W. A.: Tail Rotor Performance and Translational Flight Handling Qualities Tests of the UH-1H Helicopter. USAASTA Project #71-18, Jan. 1972.

TABLE 1.- VARIATION OF HORIZONTAL STABILIZER INCIDENCE  
WITH LONGITUDINAL STICK POSITION

cm	$\delta_e$ ,		$\delta_s$ , rad
		in.	
16.38	-6.45		0.0224
15.25	-6.00		.0174
12.7	-5.00		0
10.16	-4.00		-.0192
7.62	-3.00		-.0384
5.08	-2.00		-.0541
2.54	-1.00		-.0690
0	0		-.0820
2.54	1.00		-.0850
5.08	2.00		-.0803
7.62	3.00		-.0628
10.16	4.00		-.0300
12.7	5.00		.0035
15.25	6.00		.0593
16.38	6.45		.0942

TABLE 2.- SUMMARY OF UH-1H PHYSICAL CONSTANTS

	English	Metric
<b>Main rotor</b>		
Hub precone angle	2.75 deg	
Radius	24.13 ft	7.35 m
Chord	1.75 ft	.53 m
Tip speed ( $\Omega R$ )	760 ft/sec	231.6 m/sec
Hub station	133.5	
Hub waterline	136.5	
Solidity	.046	
<b>Tail rotor</b>		
Radius	4.25 ft	1.29 m
Chord	.70 ft	21.33 cm
Tip speed	740 ft/sec	225.5 m/sec
Shaft station	479.4	
Shaft waterline	137.5	
Solidity	.105	
<b>Center of gravity</b>		
Most forward	sta. 130	
Most aft	sta. 144	
Vertical	w.l. 55	
<b>Horizontal stabilizer</b>		
Area	16.4 ft <sup>2</sup>	1.52 m <sup>2</sup>
Span	8.75 ft	2.67 m
1/4 c station	380	
<b>Vertical fin</b>		
Area	12 ft <sup>2</sup>	1.11 m <sup>2</sup>
Span	4.5 ft	1.37 m
1/4 c station	460	
a.c., waterline	112	
<b>Fuselage</b>		
$fe_1$	19.2 ft <sup>2</sup>	1.78 m <sup>2</sup>
$C_{L\alpha}$ (includes stab.)	.036/deg	
$C_{m\alpha}$ (includes stab.)	0	
$C_{L\alpha}$ (no horiz. stab.)	.02/deg	
$C_{m\alpha}$ (no horiz. stab.)	$7.5 \times 10^{-3}$ /deg	
$S_{ref}$	48 ft <sup>2</sup>	4.46 m <sup>2</sup>
$l_{ref}$	39 ft	3.62 m
Mast tilt	+5 deg fwd.	
<b>Control travels (full throw)</b>		
Collective stick	11 in.	27.9 cm
Longitudinal stick	12.9 in.	32.8 cm
Lateral stick	12.6 in.	32.0 cm
Pedals	6.9 in.	17.5 cm
Lateral cyclic rigging	2° left	
Longitudinal cyclic pitch	+12°	
Lateral cyclic pitch	+9° to -11°	
<b>Tail rotor collective pitch</b>		
Full l. pedal	18°	
Full r. pedal	-10°	

TABLE 3.- SUMMARY OF CONSTANTS USED IN UH-IH SIMULATION

Constant	Equation/origin	Source	Simulation value	
			English	Metric
R <sub>1</sub>	$\frac{\sigma a}{2} \rho_0 A (\Omega R)^2$	Ref. 3	3.84 × 10 <sup>5</sup> lb	17.1 × 10 <sup>5</sup> N
R <sub>2</sub>	1/4Ω	Ref. 3	7.37 × 10 <sup>-3</sup> sec	7.37 × 10 <sup>-3</sup> sec
R <sub>3</sub>	1/2 a	Ref. 3	8.70 × 10 <sup>-2</sup>	
R <sub>4</sub>	1/Ω	Ref. 3	2.95 × 10 <sup>-2</sup> sec	2.95 × 10 <sup>-2</sup> sec
R <sub>5</sub>	1/4 a	Ref. 3	4.36 × 10 <sup>-2</sup>	
R <sub>6</sub>	16/γΩ	Ref. 3	.144 sec <sup>a</sup>	.144 sec
R <sub>7</sub>	1/ΩR	Ref. 3	1.22 × 10 <sup>-3</sup> sec/ft	4.00 × 10 <sup>-3</sup> sec/m
R <sub>8</sub>	$[2\rho_0 A (\Omega R)^2]^{-1}$	Ref. 3	1.715 × 10 <sup>-7</sup> 1/lb	.38 × 10 <sup>-7</sup> 1/N
R <sub>9</sub>	$\frac{\sigma a}{2} \rho_0 A (\Omega R)^2 R$	Ref. 5	9.107 × 10 <sup>6</sup> ft-lb	12.35 × 10 <sup>6</sup> J
δ <sub>0</sub>	Mean blade drag coeff. of blade section @ zero lift		.009	
δ <sub>2</sub>	$0.3 \left[ \frac{6}{\rho_0 A (\Omega R)^2 \sigma a} \right]^2$	Ref. 5	1.828 × 10 <sup>-11</sup> 1/lb <sup>2</sup>	.092 × 10 <sup>-11</sup> 1/N <sup>2</sup>
a <sub>0</sub>	Hub precone angle used as mean value for a <sub>0</sub>	Ref. 8	.048 rad	.048 rad
τ <sub>B</sub>	Constant reflects mechanical damping of stabilizer bar	Bell Heli-copter Co.	3.3 sec	3.3 sec

<sup>a</sup> Actual value should be 0.072 based on inertia of one blade. Value used was due to an error, but was retained because subjectively more realistic handling qualities resulted.

TABLE 3.- SUMMARY OF CONSTANTS USED IN UH-1H SIMULATION - Continued

Constant	Equation/origin	Source	Simulation value	
			English	Metric
$\tau_R$	$16/\gamma\Omega$	Same as $R_6$	$0.144 \text{ sec}^a$	$0.144 \text{ sec}$
$\tau_C$	Used to match flight test data	This simulation	$.20 \text{ sec}$	$.20 \text{ sec}$
$K_B$	Product of stabilizer bar linkage geometry and $\tau_B$	Bell Helicopter Co. Thus, $K_B = 0.528 \text{ sec}$	$K_B = K_\ell \tau_B \text{ sec}$ $K_\ell = 0.16$	$.528 \text{ sec}$ $.528 \text{ sec}$
$C_1$	Long. cyclic/unit of stick	Ref. 9	$.0324 \text{ rad/in.}$	$.0127 \text{ rad/cm}$
$C_4$	Lateral cyclic/unit stick	Ref. 9	$.0277 \text{ rad/in.}$	$.0109 \text{ rad/cm}$
$C_5$	Collective pitch per in. of stick	Ref. 9	$.025 \text{ rad/in.}$	$.0098 \text{ rad/cm}$
$\ell_H$	Estimated for this simulation	---	$6.79 \text{ ft}$	$2.07 \text{ m}$
$\ell_{TR}$	Assumed constant	Ref. 9	$28.0 \text{ ft}$	$8.53 \text{ m}$
$X_{c.g.}$	Variable $-0.520$ used for sim.	Ref. 9	$-.541 \text{ ft}$ (flt. test.)	$.165 \text{ m}$
$\ell_{VF}$	Assumed constant	Ref. 9	$25.0 \text{ ft}$	$7.62 \text{ m}$
$C_6$	Tail rotor collective to pedal motion	Ref. 9	$-.071 \text{ rad/in.}$	$-.028 \text{ rad/cm}$
$C_7$	Tail rotor collective for zero pedal	Ref. 9	$.119 \text{ rad}$	$.119 \text{ rad}$

TABLE 3.- SUMMARY OF CONSTANTS USED IN UH-1H SIMULATION - Continued

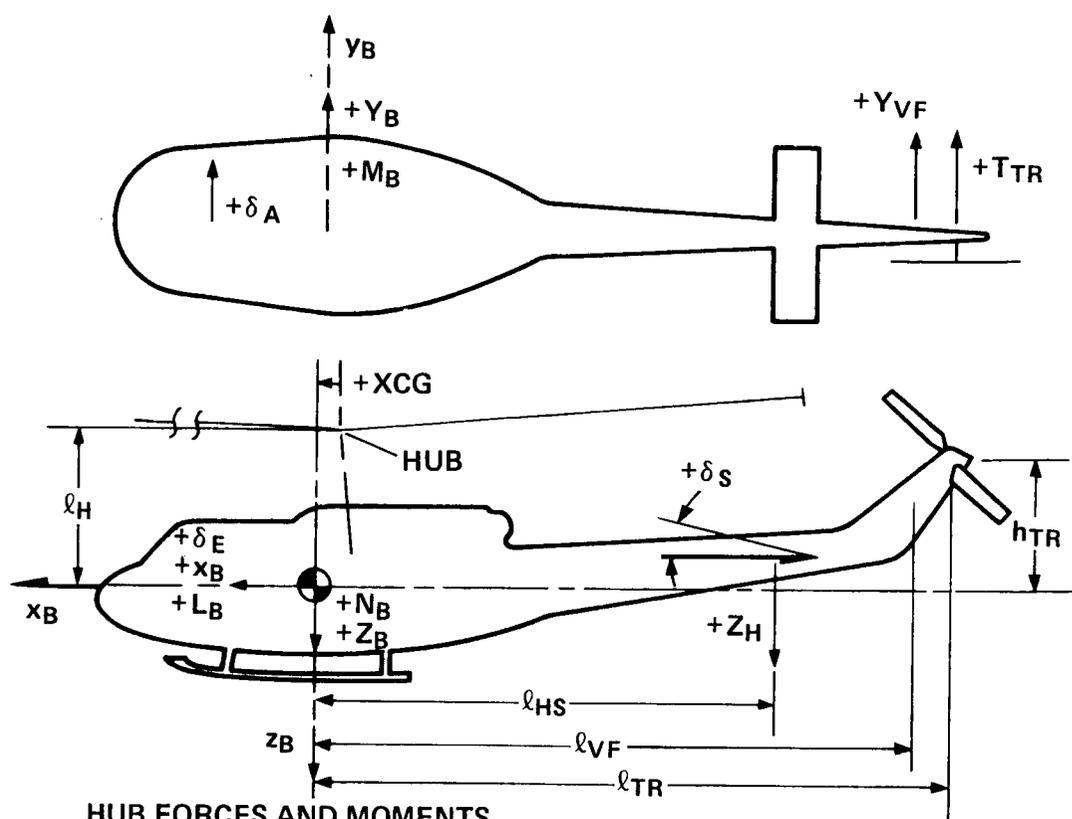
Constant	Equation/origin	Source	Simulation value	
			English	Metric
$h_{TR}$	Estimated for this simulation		6.88 ft	2.10 m
$l_{HS}$	Assumed constant	Ref. 9	19.67 ft	6.0 m
$T_1$	$\frac{1}{2(\Omega R)TR}$	This simulation	$6.76 \times 10^{-4}$ sec/ft	$22.17 \times 10^{-4}$ sec/m
$T_2$	$\left[ \frac{\rho_0 A (\Omega R)^2}{TR} \right]^{1/2} \frac{(\alpha \sigma) TR}{8\sqrt{2}}$	This sim. (adjusted to match test).	17.0 lb <sup>1/2</sup>	35.7 N <sup>1/2</sup>
$T_3$	$\left[ \frac{\rho_0 A (\Omega R)^2}{TR} \right] \frac{(\alpha \sigma) TR}{6}$	This sim. (adjusted to match test).	$7.0 \times 10^3$ lb	$31.1 \times 10^3$ N
$T_4$	---	This sim. (adj. to match test).	14.9 lb/ft	217.4 N/m
$T_5$	---	This sim. (adj. to match test).	0	0
$D_1$	$\frac{1}{2} \rho_0 f e_1$	Ref. 4	$.022 \frac{lb}{(ft/sec)^2}$	$1.05 \frac{N}{(m/sec)^2}$
$D_2$	$\frac{1}{2} \rho_0 f e_2$	Estimated for this sim.	$.201 \frac{lb}{(ft/sec)^2}$	$9.62 \frac{N}{(m/sec)^2}$
$D_3$	$\frac{1}{2} \rho_0 f e_3$	Est. for this sim.	$.646 \frac{lb}{(ft/sec)^2}$	$30.92 \frac{N}{(m/sec)^2}$
$L_1$	$\left( \rho_0 S_{ref} C_{L\alpha_{FUS}} \right) / 2$	This sim. and ref. 4	$6.54 \times 10^{-2} \frac{lb}{(ft/sec)^2}$	$3.13 \frac{N}{(m/sec)^2}$
$Y_1$	Assumed same as $L_1$		$6.54 \times 10^{-2} \frac{lb}{(ft/sec)^2}$	$.29 \frac{N}{(m/sec)^2}$

TABLE 3.- SUMMARY OF CONSTANTS USED IN UH-1H SIMULATION - Continued

Constant	Equation/origin	Source	Simulation value	
			English	Metric
$M_1$	$\frac{1}{2} \rho_0 S_{ref}^{\ell} C_m^{\alpha_{FUS}}$	This simulation and ref. 4	$0.956 \frac{\text{ft-lb}}{(\text{ft/sec})^2}$	$13.95 \frac{\text{J}}{(\text{m/sec})^2}$
$N_1$	Assumed same as $L_1$		$.956 \frac{\text{ft-lb}}{(\text{ft/sec})^2}$	$13.95 \frac{\text{J}}{(\text{m/sec})^2}$
$H_1$	$\frac{1}{2} \rho_0 S_{HS} C_L^{\alpha_{HS}}$	Adjusted to match flt. data	$.031 \frac{\text{lb}}{(\text{ft/sec})^2}$	$1.48 \frac{\text{N}}{(\text{m/sec})^2}$
$H_2$	$H_1 \tan 20^\circ$	This simulation	$.01128 \frac{\text{lb}}{(\text{ft/sec})^2}$	$.54 \frac{\text{N}}{(\text{m/sec})^2}$
$H_4$	$\frac{1}{2} \rho_0 S_{HS} C_D^{\alpha} = 90^\circ$	Adjusted to match test data	$.0083 \frac{\text{lb}}{(\text{ft/sec})^2}$	$.40 \frac{\text{N}}{(\text{m/sec})^2}$
$F_1$	$\frac{1}{2} \rho_0 S_{FIN} C_D^{\alpha} = 90^\circ$	Adjusted to match test data	$.016 \frac{\text{lb}}{(\text{ft/sec})^2}$	$.77 \frac{\text{N}}{(\text{m/sec})^2}$
$k_1$	$\frac{1}{2} \rho_0 S_{FIN} C_L^{\alpha_{FIN}}$	Adjusted to match test data	$.0292 \frac{\text{lb}}{(\text{ft/sec})^2}$	$1.40 \frac{\text{N}}{(\text{m/sec})^2}$
$k_2$	$k_1 \tan 20^\circ$	This simulation	$.0106 \frac{\text{lb}}{(\text{ft/sec})^2}$	$.51 \frac{\text{N}}{(\text{m/sec})^2}$
$A_{1CL}$	Rigging constant - lateral cyclic pitch	Adjusted to match BHG data	$-.0486 \text{ rad}$	$-.0486 \text{ rad}$
$B_{1CL}$	Rigging constant - long. cyclic pitch	Adjusted to match BHG data	$.081 \text{ rad}$	$.081 \text{ rad}$
$G_1$	Approximation to account for ground effect	Ref. 6	$.28$	

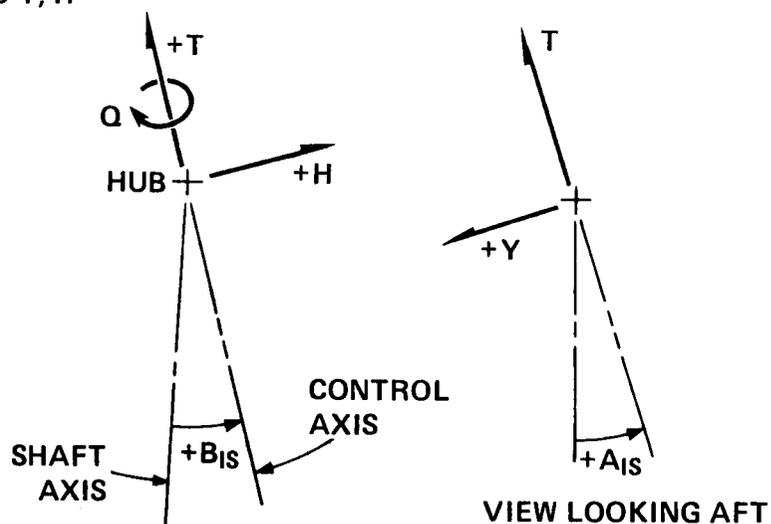
TABLE 3.- SUMMARY OF CONSTANTS USED IN UH-1H SIMULATION - Concluded

Constant	Equation/origin	Source	Simulation value	
			English	Metric
Weight		Measurement	6158 (valid) lb 8700 (sim) lb	27,391 N 38,698 N
$I_{xx}$		Bell Helicopter Co. data	2800 slug-ft <sup>2</sup>	3795 kg-m <sup>2</sup>
$I_{yy}$		Bell Heli- copter Co. data	12,733 slug-ft <sup>2</sup>	17,259 kg-m <sup>2</sup>
$I_{zz}$		Bell Heli- copter Co. data	10,800 slug-ft <sup>2</sup>	14,639 kg-m <sup>2</sup>
$I_{xz}$		Bell Heli- copter Co. data	1480 slug-ft <sup>2</sup>	2006 kg-m <sup>2</sup>



**HUB FORCES AND MOMENTS**

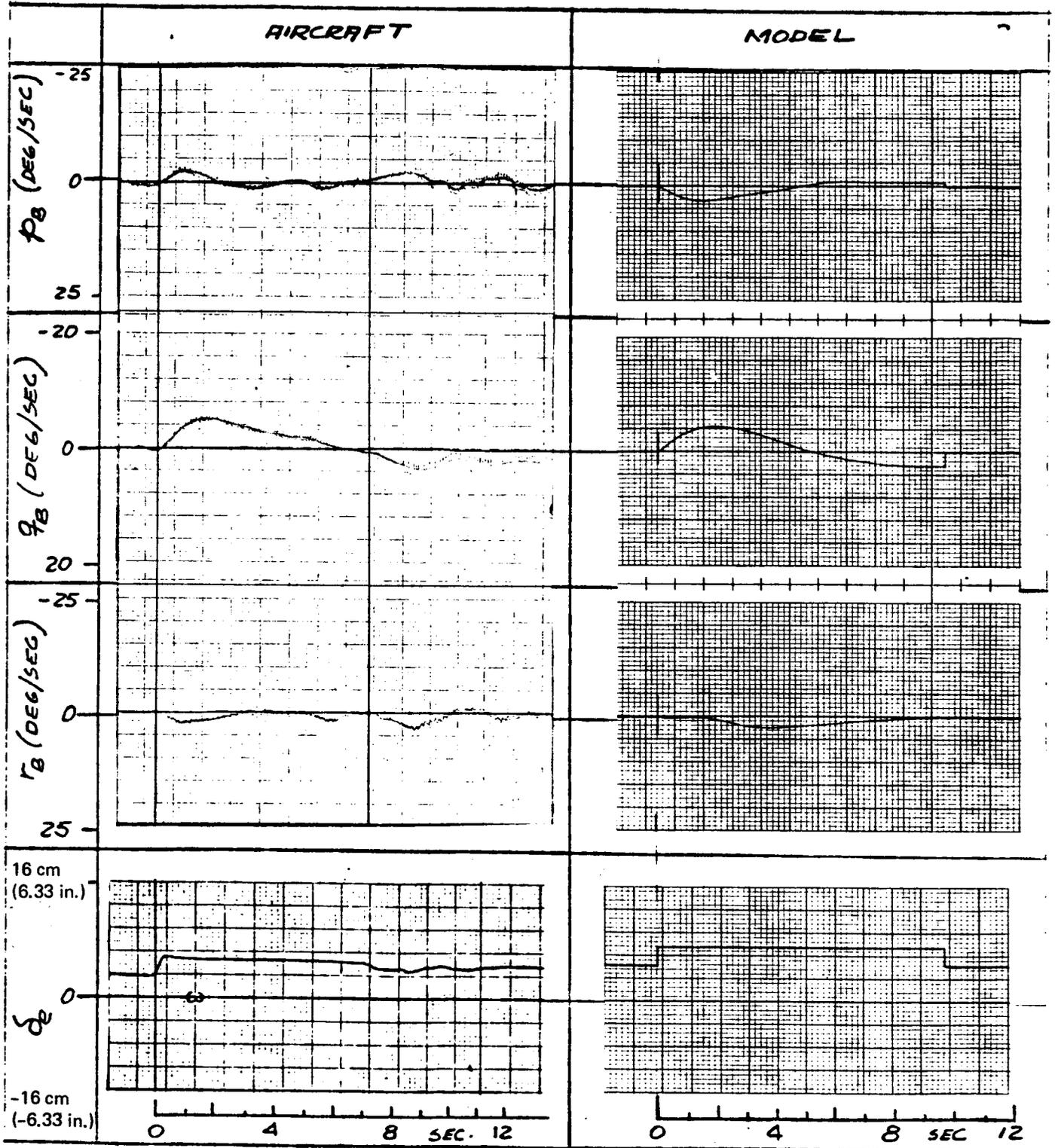
- T - ALONG CONTROL AXIS
- H - NORMAL TO CONTROL AXIS IN PLANE OF RELATIVE WIND AND CONTROL AXIS
- Y - NORMAL TO T, H



**NOTE: BODY Z AXIS IS PARALLEL TO MAIN ROTOR SHAFT**

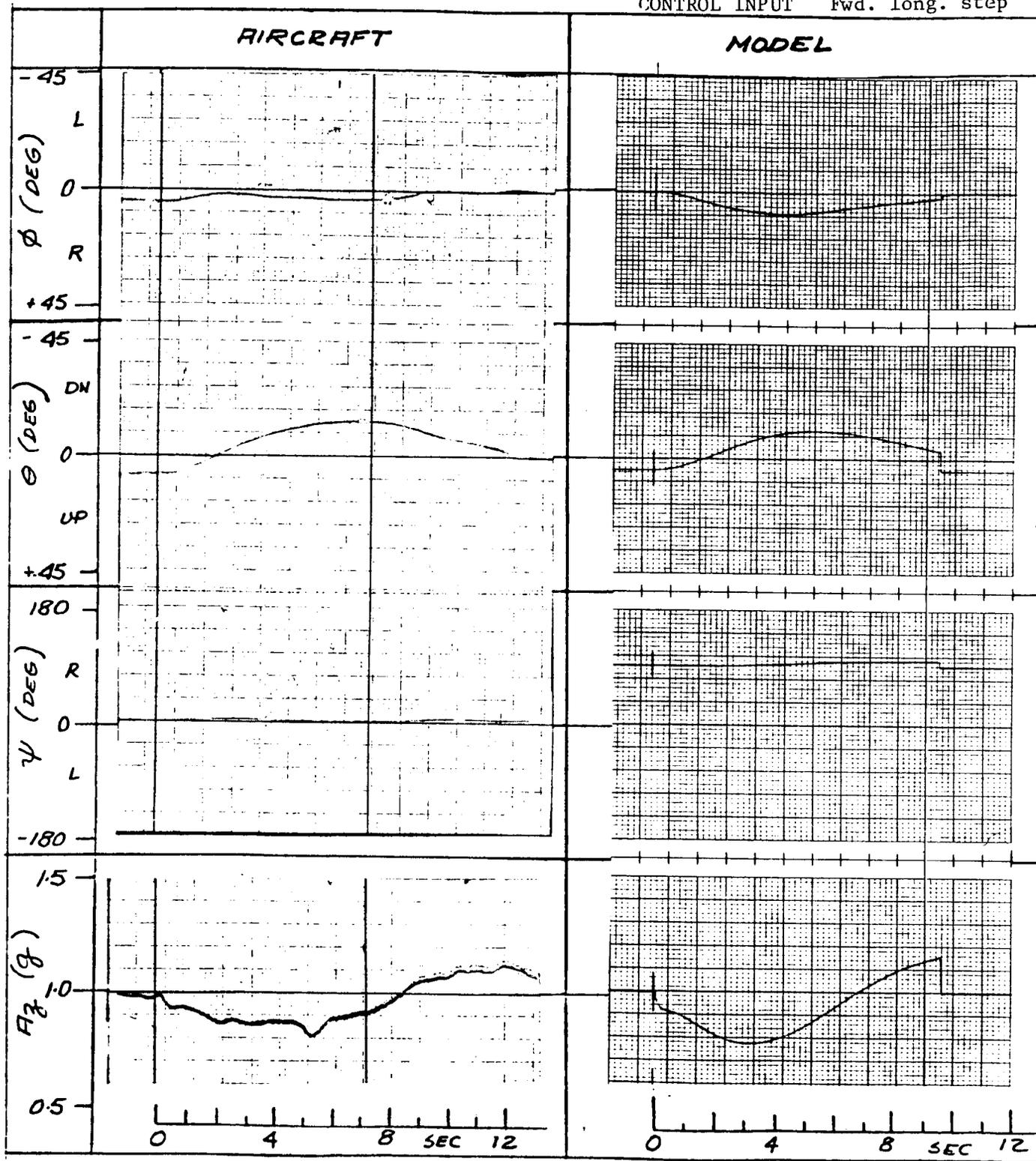
Figure 1.- Characteristic lengths and sign conventions used for forces, moments and control displacements.

AIRCRAFT UH-1H SN AAB-11519  
 CONTROL INPUT Fwd. long. step  
 FLIGHT CONDITION 60 knots  
 GROSS WEIGHT 29,371 N (6158 lb)  
 LONGITUDINAL CG.



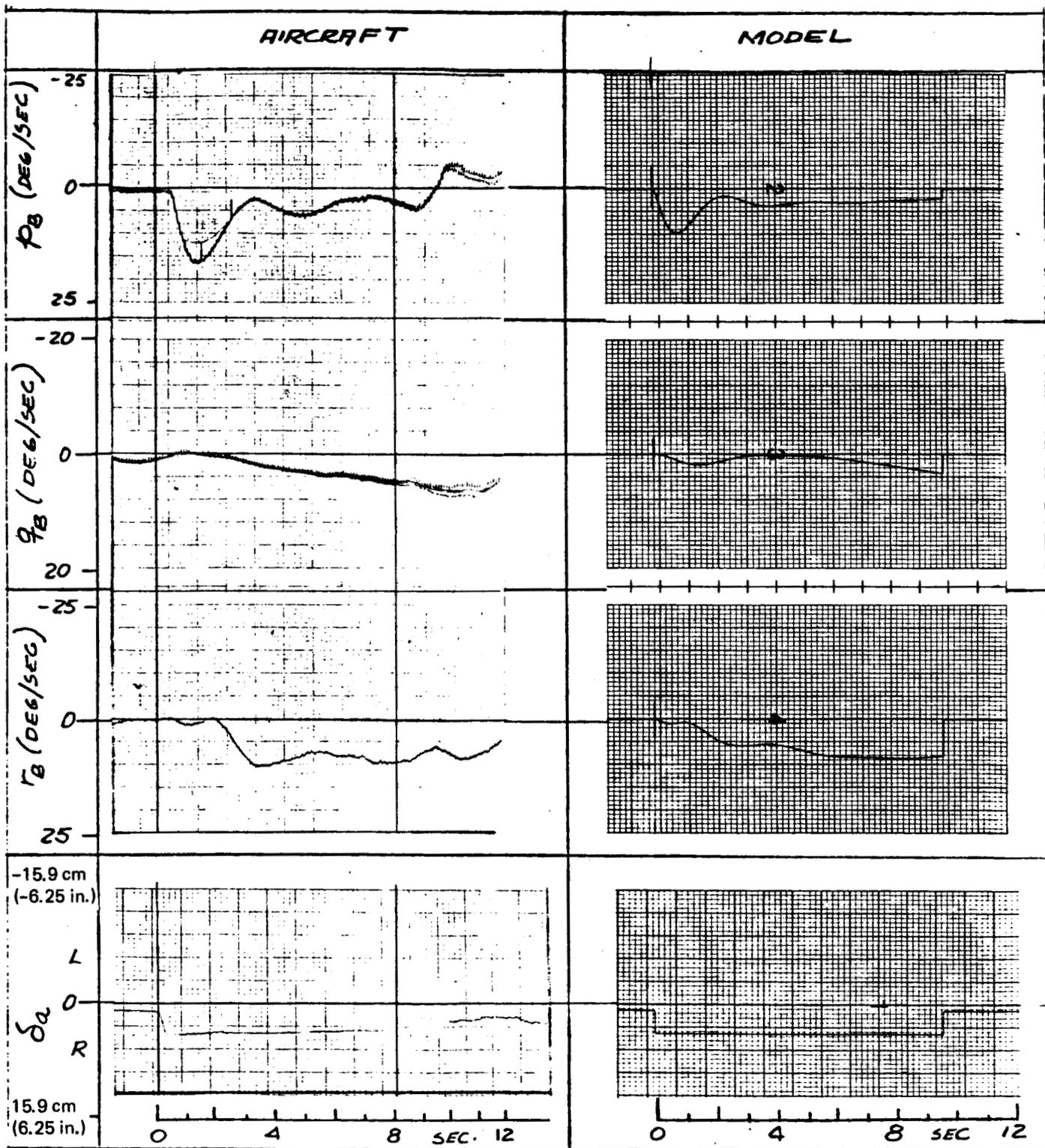
(a) Rate response.

Figure 2.- Forward cyclic step input.



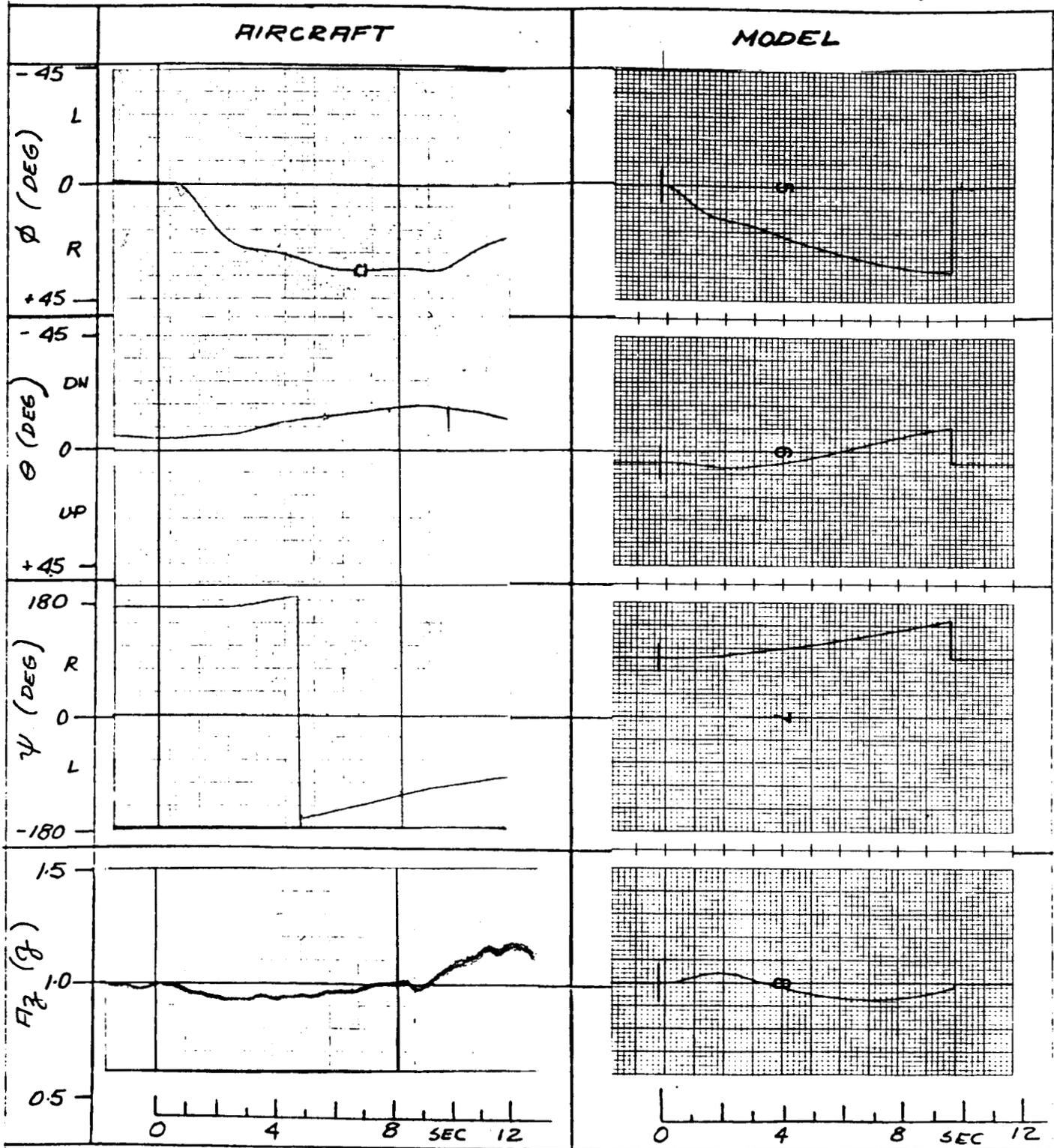
(b) Attitude response.

Figure 2.- Concluded.



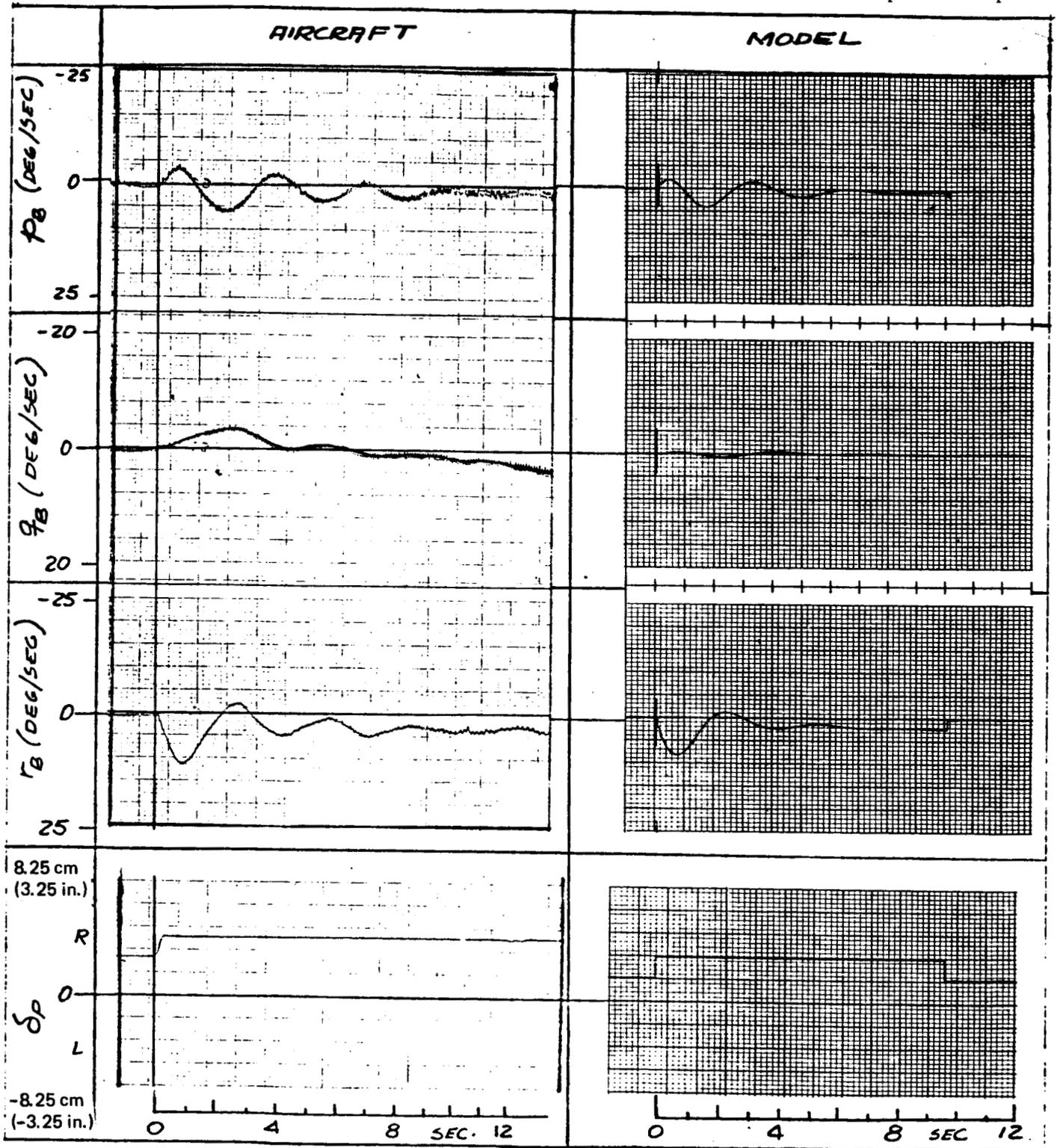
(a) Rate response.

Figure 3.- Lateral step input.



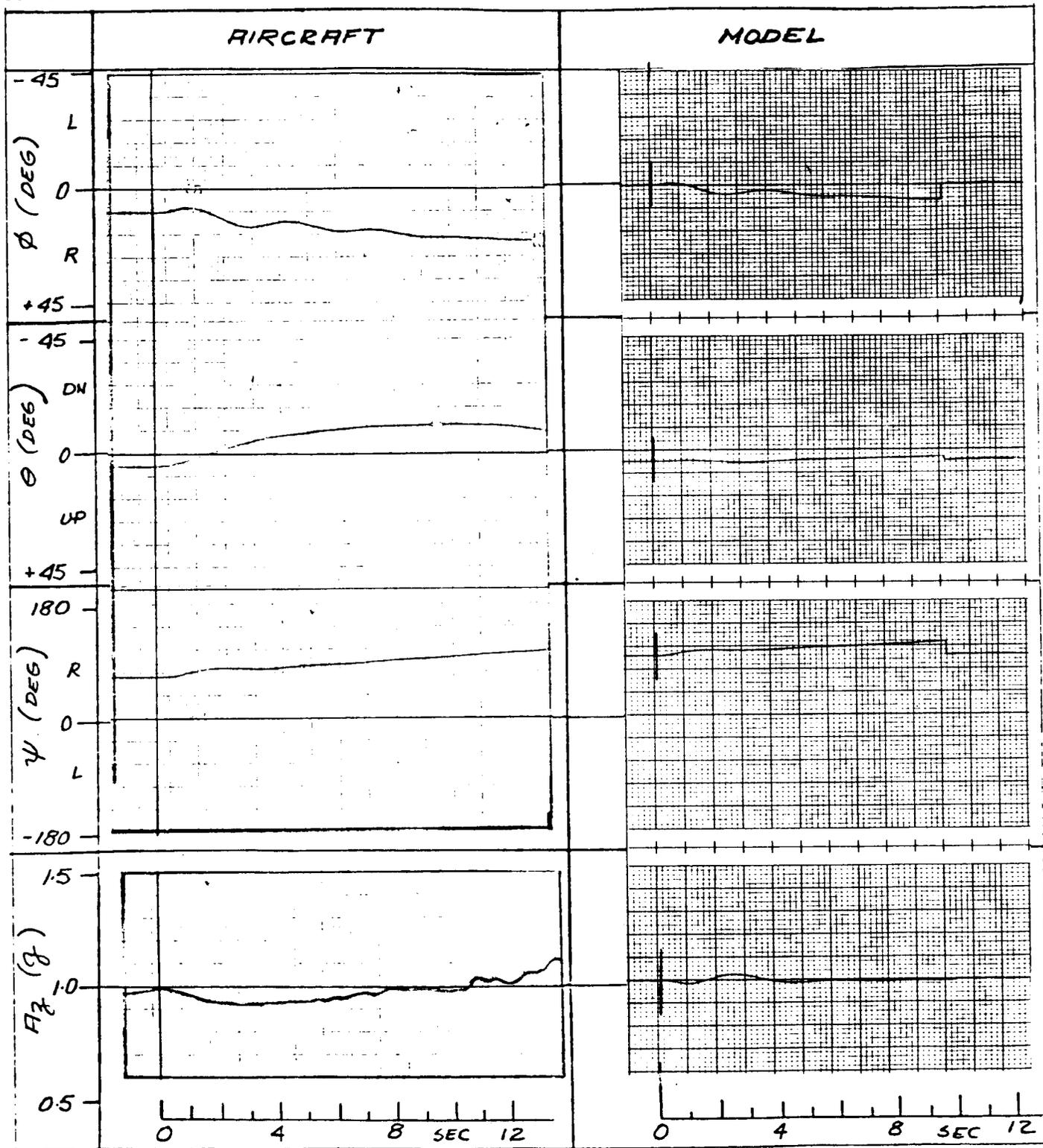
(b) Attitude response.

Figure 3.- Concluded.



(a) Rate response.

Figure 4.- Pedal step input.

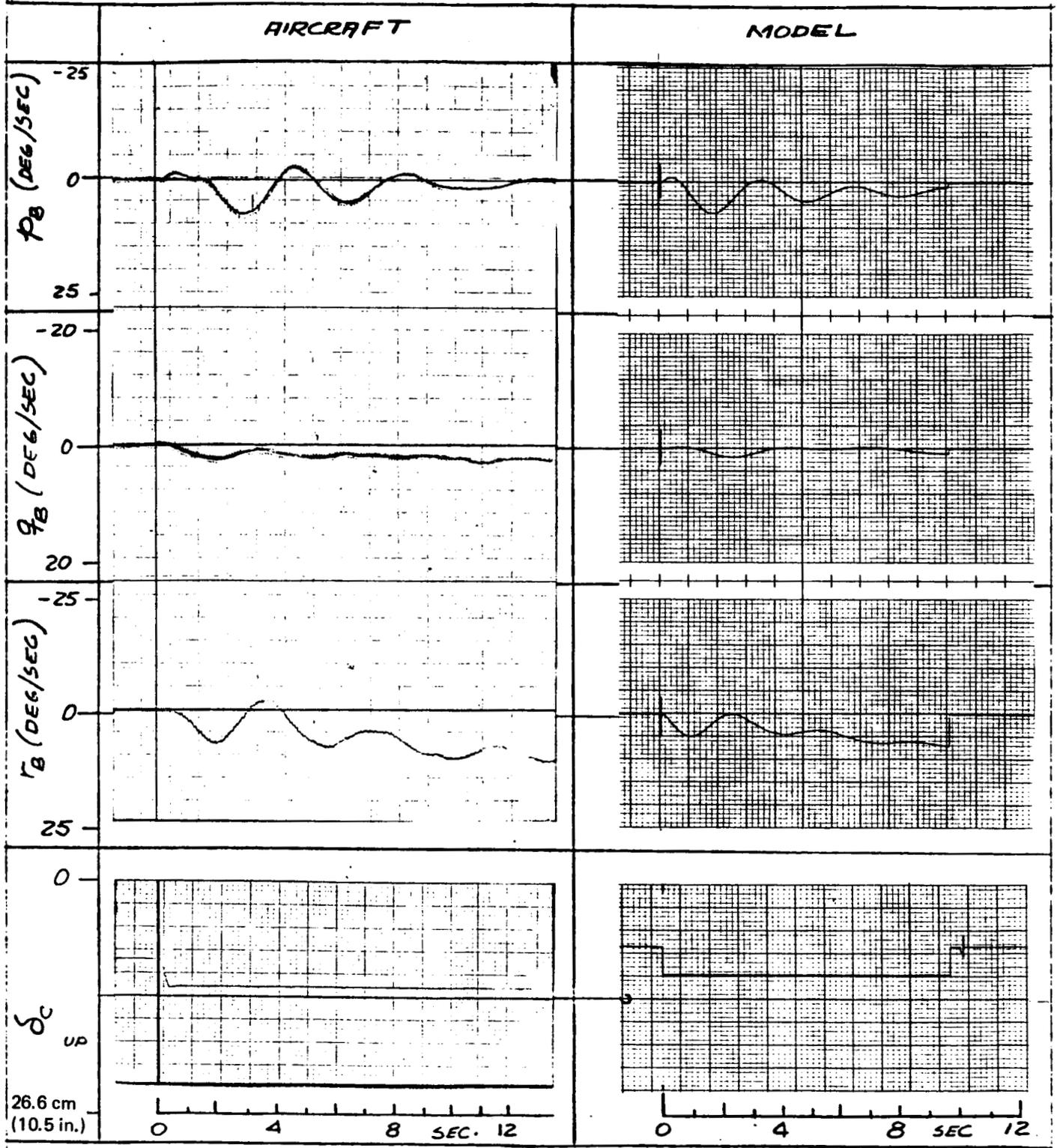


(b) Attitude response.

Figure 4.- Concluded.

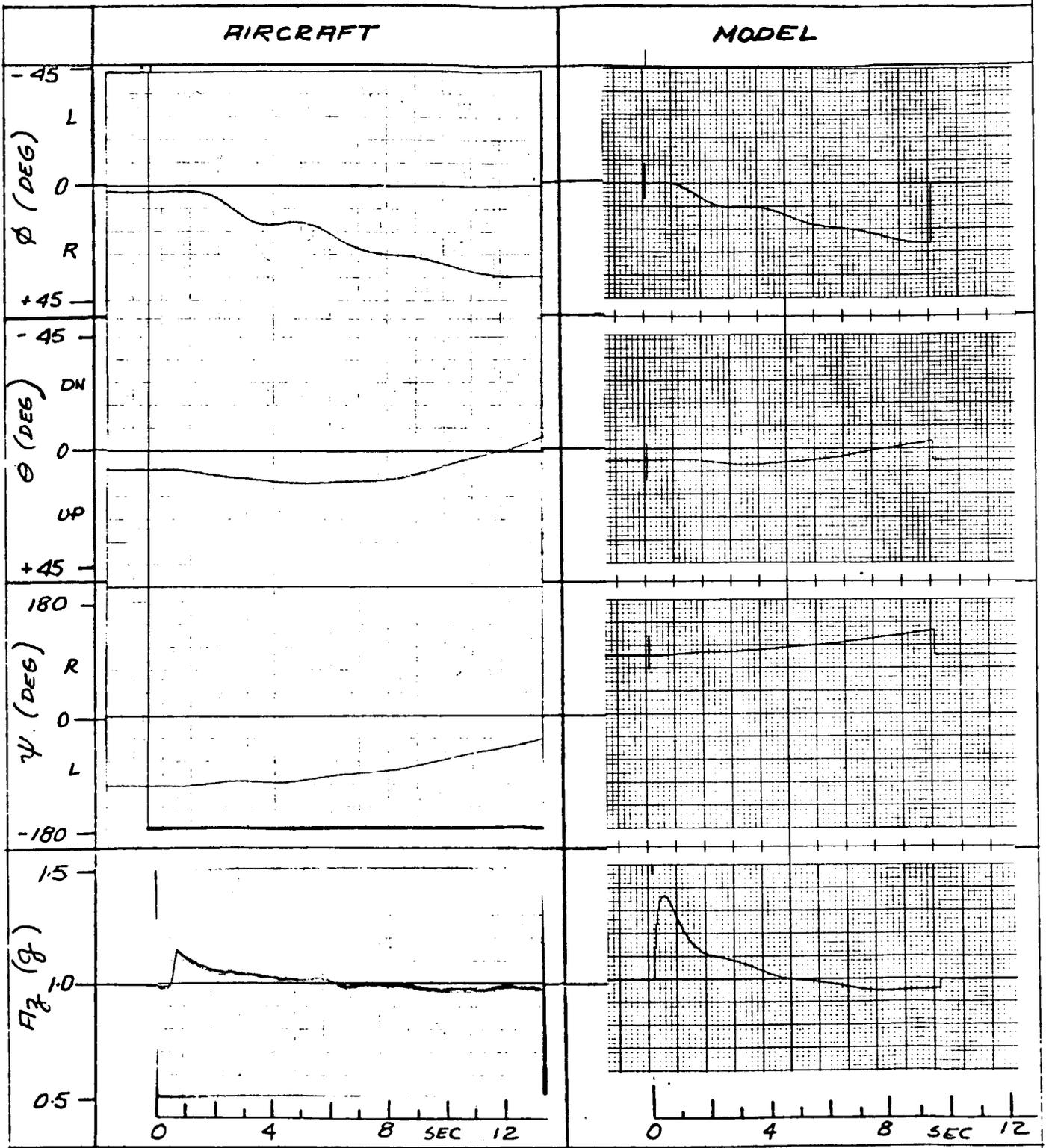
60 KNOTS

CONTROL INPUT UP collective



(a) Rate response.

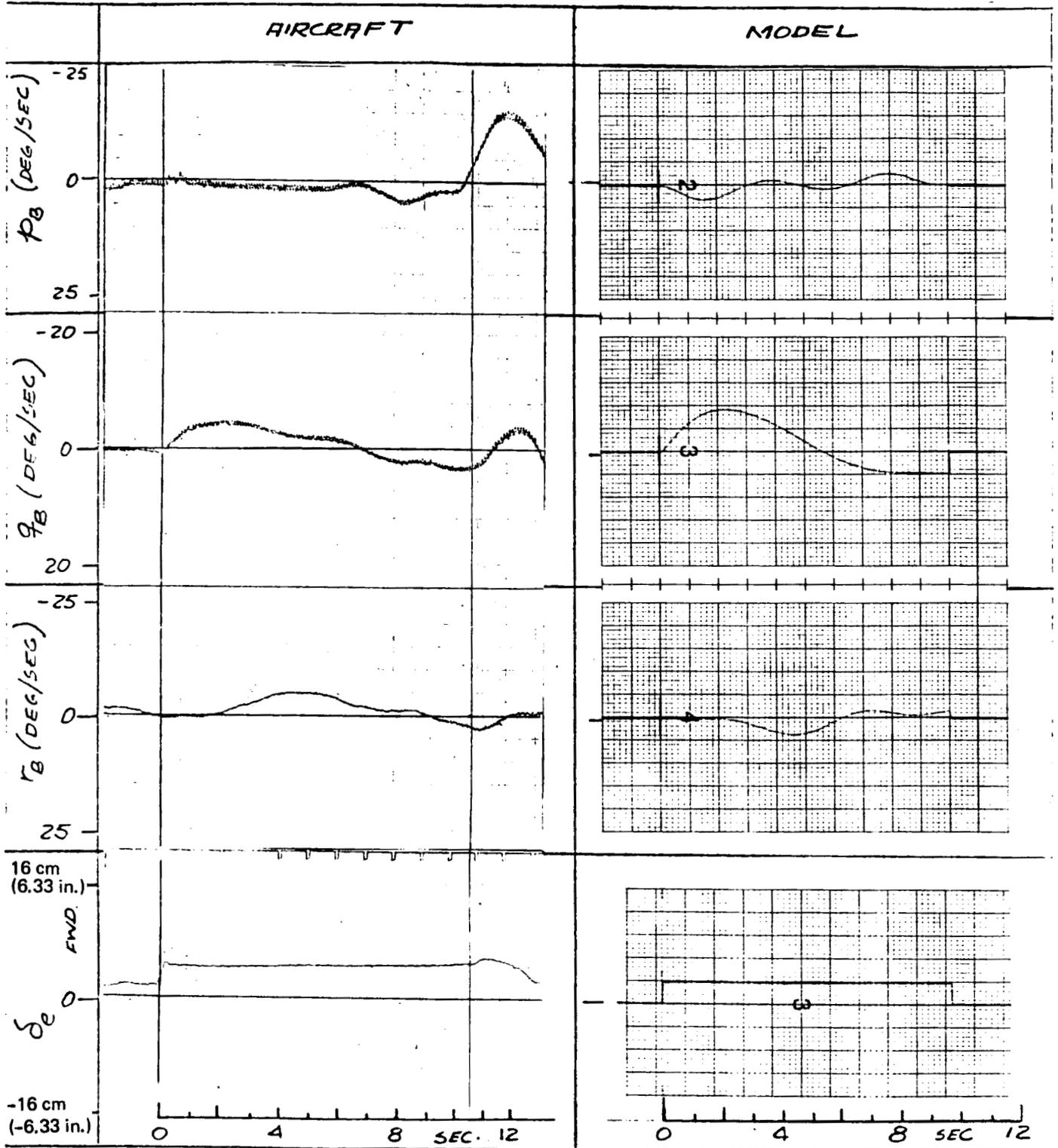
Figure 5.- Collective step input.



(b) Attitude response.

Figure 5.- Concluded.

AIRCRAFT UH-1H SN AAB-11519  
 CONTROL INPUT Fwd. long. step  
 FLIGHT CONDITION Hover  
 GROSS WEIGHT 29,371 N (6158 lb)  
 LONGITUDINAL CG.

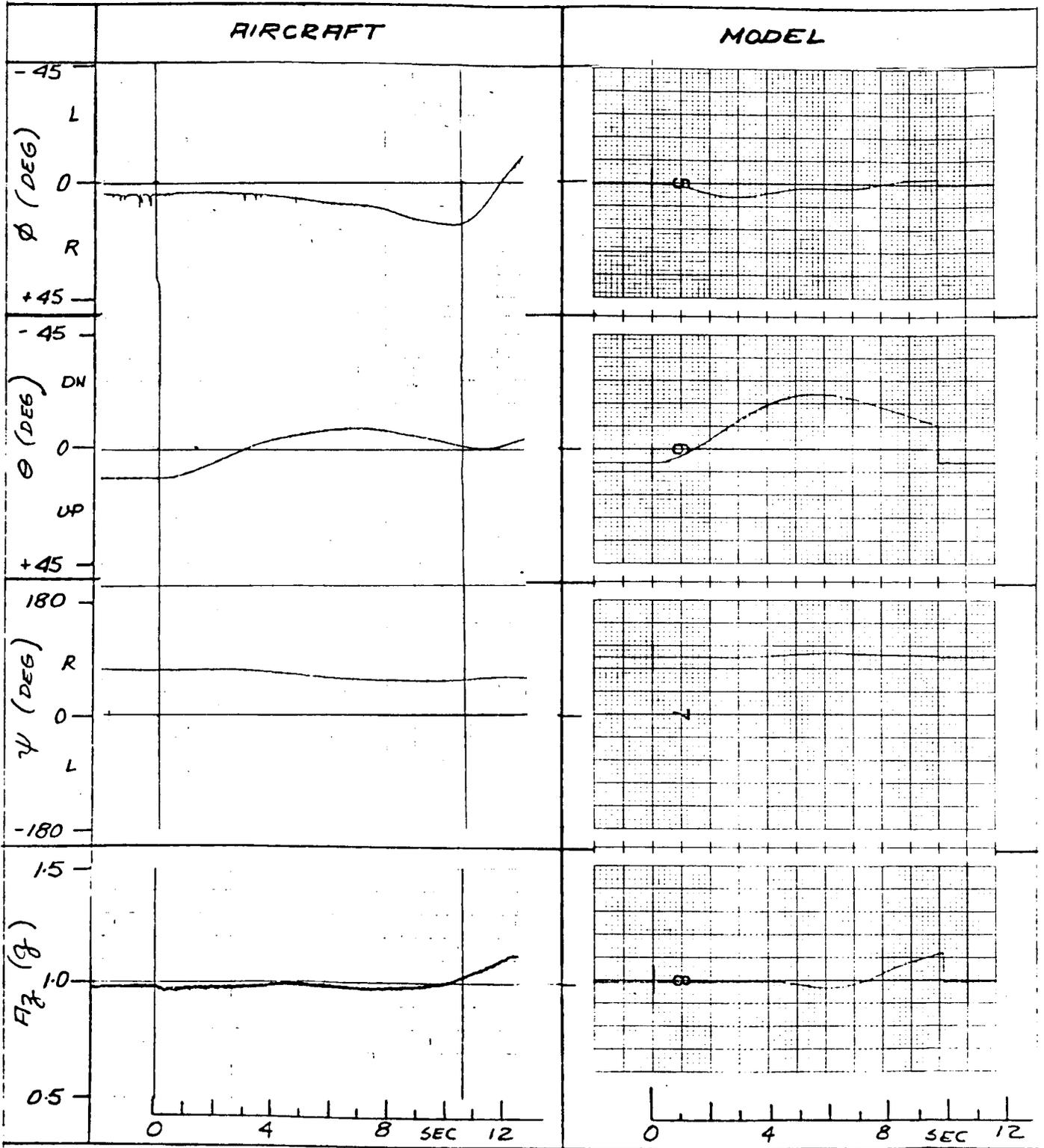


(a) Rate response.

Figure 6.- Forward cyclic step input.

HOVER

CONTROL INPUT Fwd. long. step

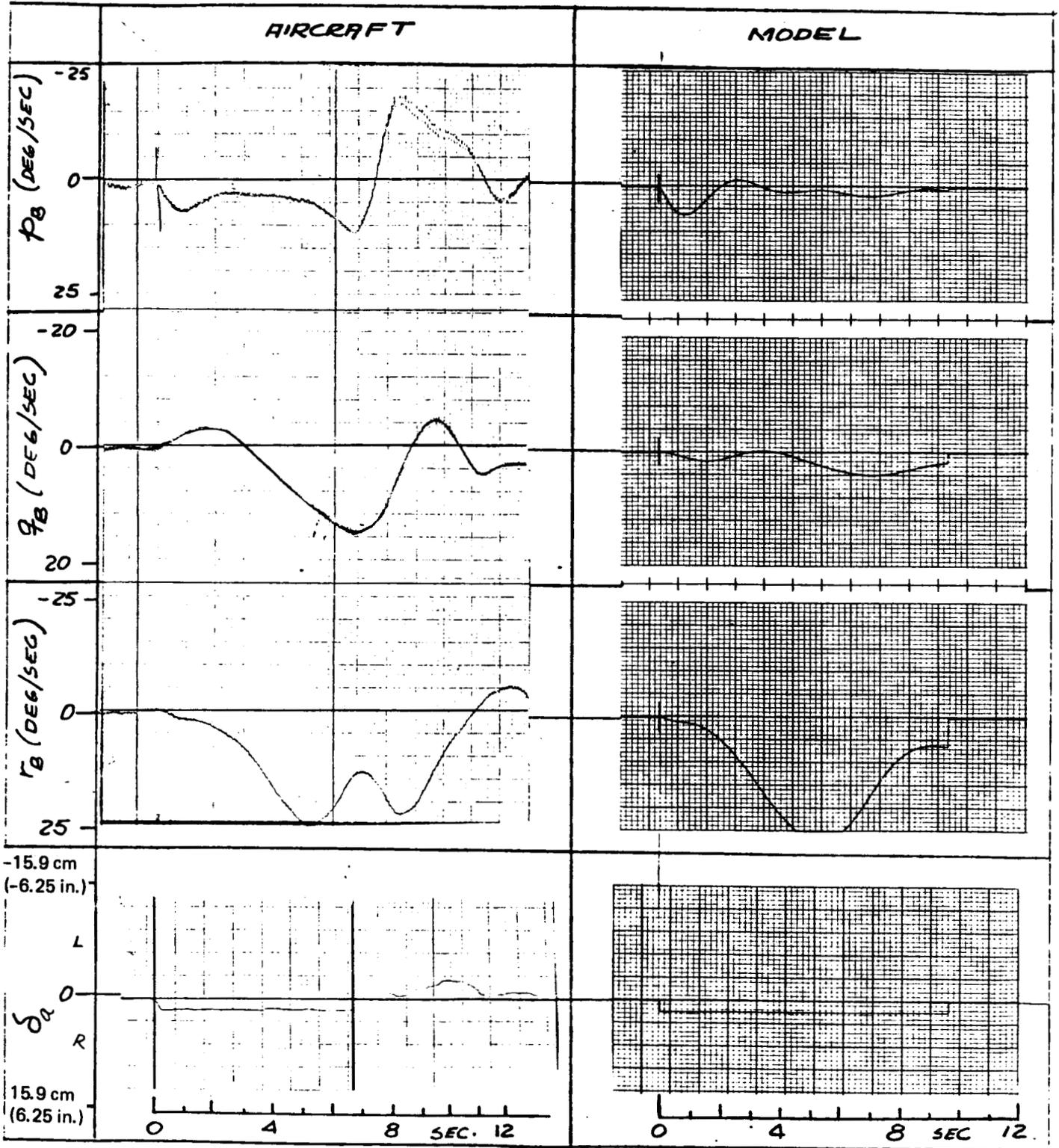


(b) Attitude response.

Figure 6.- Concluded.

HOVER

CONTROL INPUT Lat. cyclic step

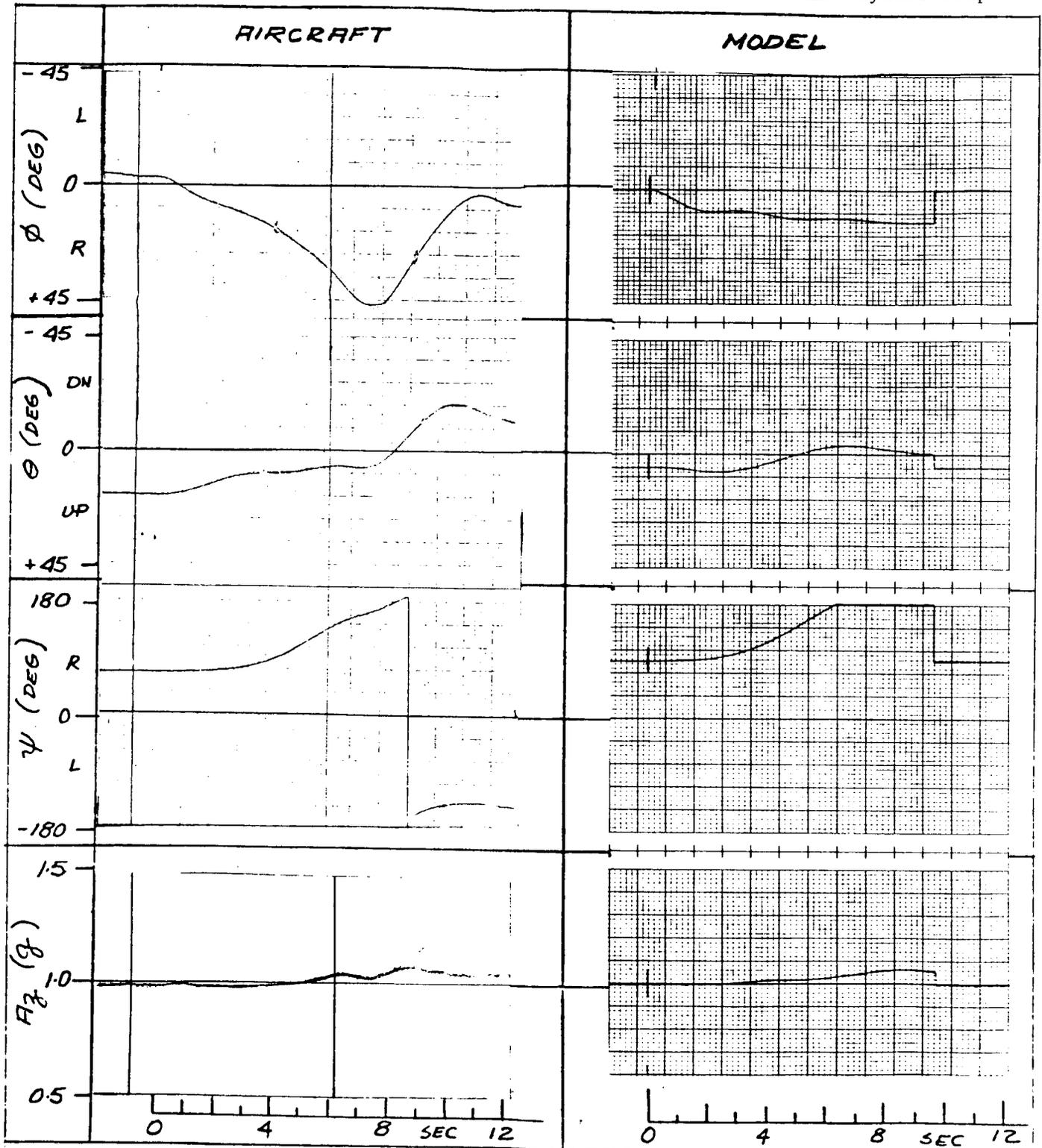


(a) Rate response.

Figure 7.- Lateral cyclic step input.

HOVER

CONTROL INPUT Lat. cyclic step

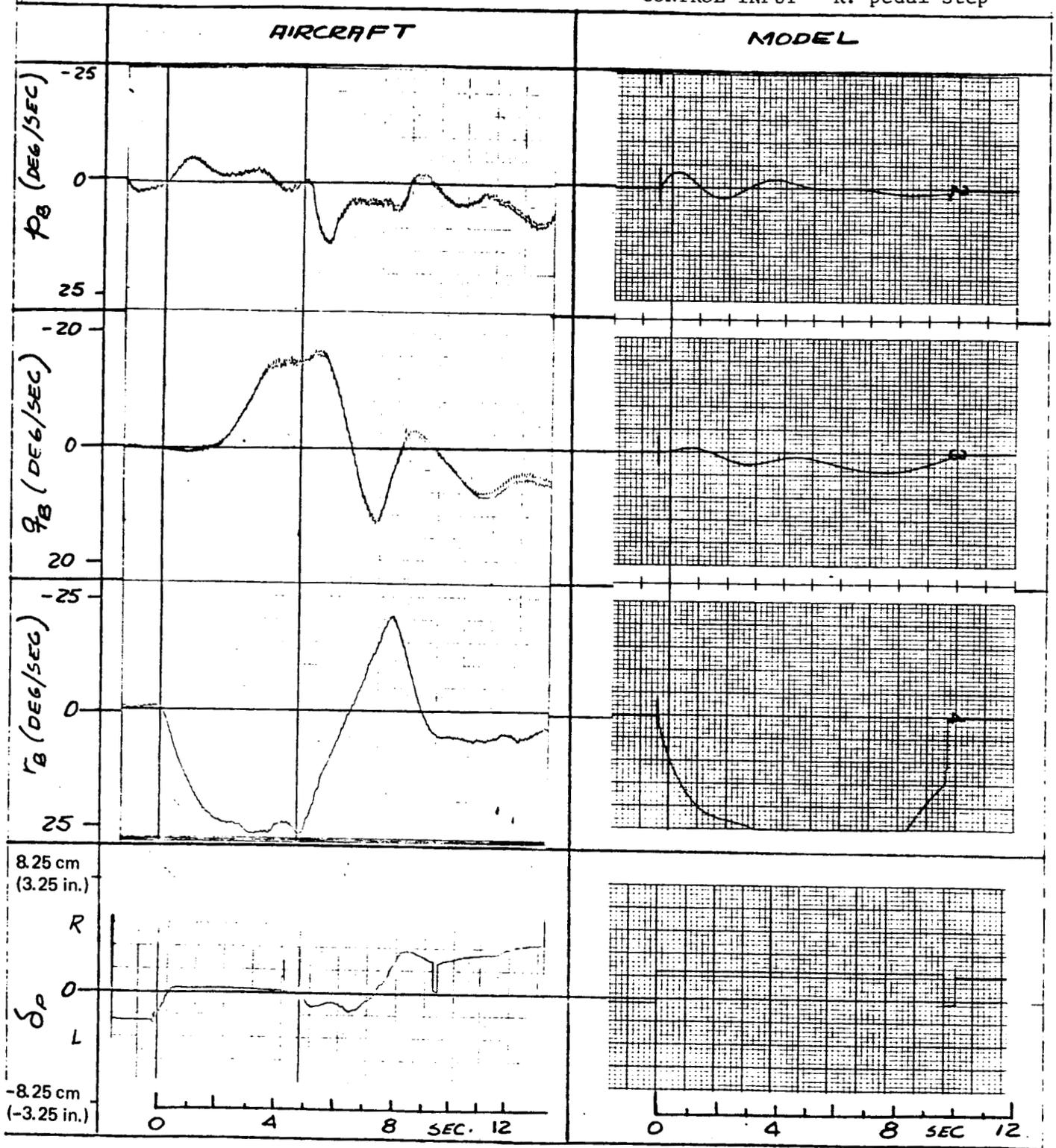


(b) Attitude response.

Figure 7.- Concluded.

HOVER

CONTROL INPUT R. pedal step

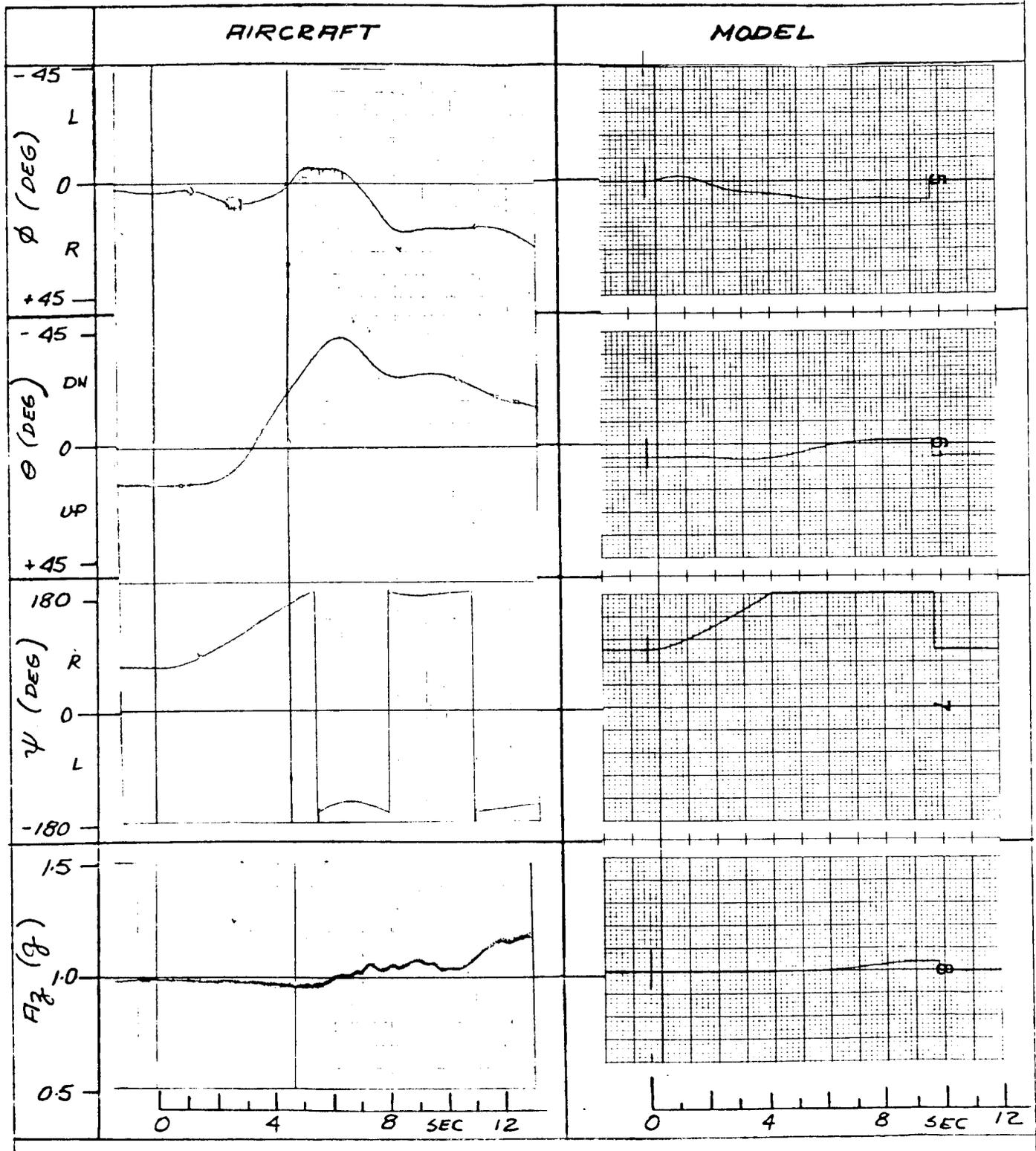


(a) Rate response.

Figure 8.- Pedal step input.

HOVER

CONTROL INPUT R. pedal step

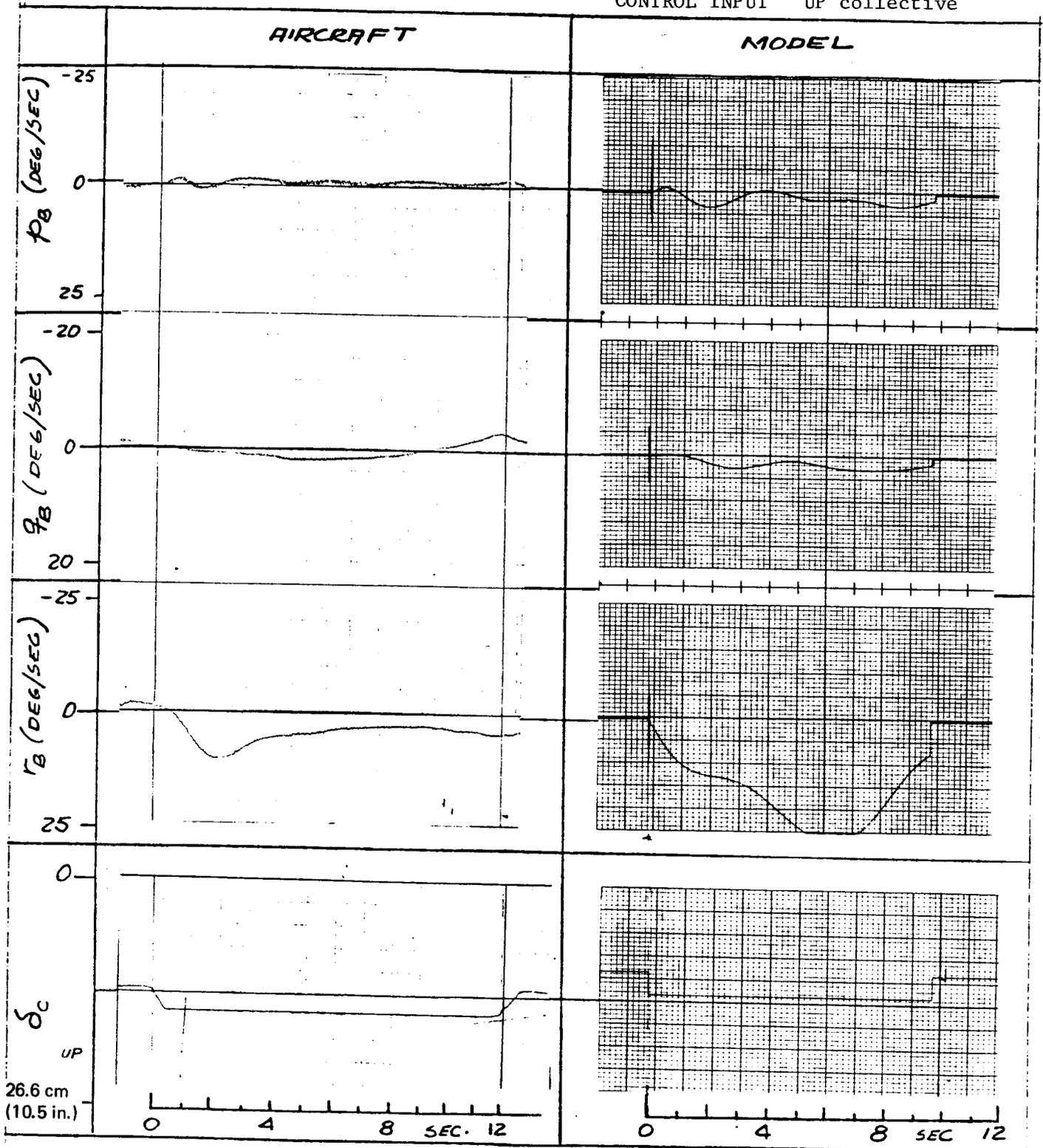


(b) Attitude response.

Figure 8.- Concluded.

HOVER

CONTROL INPUT UP collective

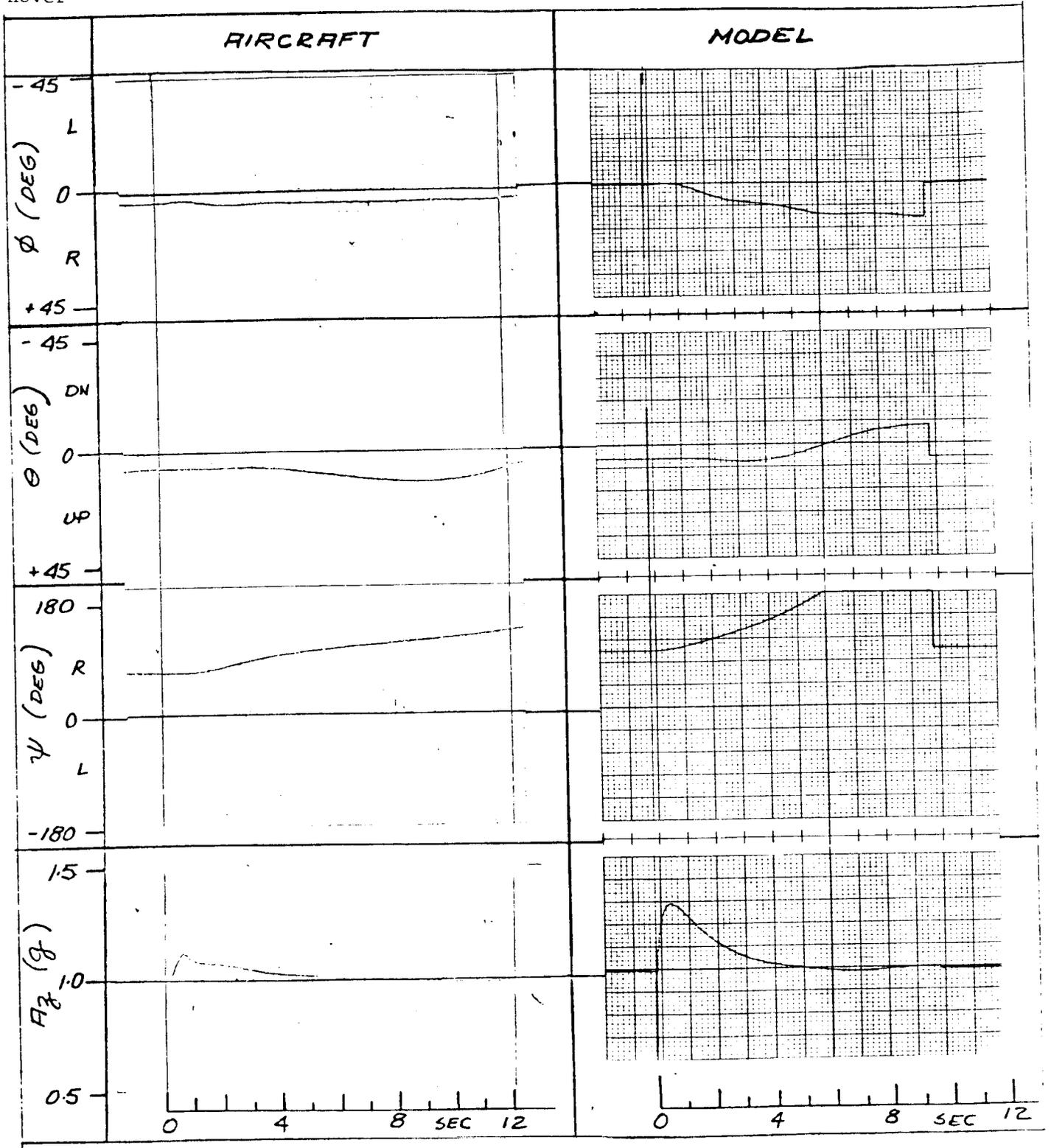


(a) Rate response.

Figure 9.- Collective step input.

Hover

CONTROL INPUT UP collective



(b) Attitude response.

Figure 9.- Concluded.

1. Report No. TM-73,254	2. Government Accession No.	3. Recipient's Catalog No.	
4. Title and Subtitle A MATHEMATICAL FORCE AND MOMENT MODEL OF A UH-1H HELICOPTER FOR FLIGHT DYNAMICS SIMULATIONS		5. Report Date	
		6. Performing Organization Code	
7. Author(s) Peter D. Talbot and Lloyd D. Corliss		8. Performing Organization Report No. A-7080	
		10. Work Unit No. 505-10-23	
9. Performing Organization Name and Address Ames Research Center, NASA and Ames Directorate, USAAMRDL, AVRADCOM, Ames Research Center Moffett Field, CA 94035		11. Contract or Grant No.	
		13. Type of Report and Period Covered Technical Memorandum	
12. Sponsoring Agency Name and Address National Aeronautics and Space Administration Washington, D. C. 20546 and U.S. Army Air Mobility R&D Laboratory, Moffett Field, CA 94035		14. Sponsoring Agency Code	
		15. Supplementary Notes	
16. Abstract  <p>A model of a Bell UH-1H helicopter was developed to support several simulations at Ames Research Center and was used also for development work on an avionics system known as the V/STOLAND system at Sperry Flight Systems. This report presents the complete equations and numerical values of constants used to represent the helicopter.</p> <p>Responses to step inputs of the cyclic and collective controls are shown and compared with flight test data for a UH-1H. The model coefficients were adjusted in an attempt to get a consistent match with the flight time histories at hover and 60 knots. Fairly good response matching was obtained at 60 knots, but the matching at hover was not as successful. Pilot evaluations of the model, both fixed and moving base, were made.</p>			
17. Key Words (Suggested by Author(s)) UH-1H helicopter flight dynamics Simulation Fixed base and comparison with flight test		18. Distribution Statement  Unlimited  STAR Category - 08	
19. Security Classif. (of this report) Unclassified	20. Security Classif. (of this page) Unclassified	21. No. of Pages 45	22. Price* \$3.75